#### HYDRAULIC BEHAVIOUR OF SIDE-WEIRS

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In Partial Fulfilment of the Requirements

For the Degree of

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POST GRADUATE OFFICE

This thesis has been approved for the award of the Degree of Master of Lech 10 03y (M Tech)

# in accordance with the

regulations of the Indian factions of Technology Lanpur

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SUBHASH CHANDRA AWASTHY

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INDIAN INSTITUTE OF TECHNOLOGY, KANPUR
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#### CERTIFICATE

This is to certify that the thesis entitled 'HYDRAULIC BEHAVIOUR OF SIDE-WEIRS' by SUBHASH CHANDRA AWASTHY is record of work carried out under my supervision and has not been submitted elsewhere for a degree.

Dr. K. Subramanya
Assistant Professor
Civil Engineering Dept.

Indian Institute of Technology
Kanpur

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# NOMENCLATURE

A	area of the flow section					
B	width of the channel					
$\mathbb{B}_{\mathbf{w}}$	width of the water surface at Weir level					
G	a coefficient					
CII	a coefficient					
Ca	a coefficient					
Ср	a coefficient					
Cd	a coefficient					
$\mathrm{c}^{\mathrm{M}}$	a coefficient					
C <sub>M</sub> ∗	a constant coefficient					
D	diameter of the pipe					
D	hydraulic depth					
E	specific energy					
$\mathbf{E}_{\mathbf{w}}$	specific energy with reference to Weir Crest level					
F	Froude number					
F <sub>1</sub>	upstream Froude number					
F <sub>2</sub>	down stream Froude number					
f <sub>1</sub>	a function					
fn	a function					
fn'	a function					
g	acceleration due to gravity					
H	total head					
h <sub>1</sub>	upstream depth over the weir crest					

downstream depth over the weir crest

h<sub>2</sub>

```
a constant
K
\mathbf{L}
          length of the side-weir
          rugosity coefficient
n
          an exponent
q
          flow through a section
Q
          upstream flow
Q1
          downstream flow
Q_2
          available flow
Q_{\mathbf{a}}
          flow in the channel when the weir starts functioning
Qn
          total flow over the side-weir
Q_{\mathbf{g}}
          upstream design discharge
Q_{\Omega}
          an exponent
q
          discharge per unit width over the side-weir
q_{s}
R
          hydraulic radius
          an exponent
r
           friction slope
Sf
           bed slope
S
           height of the weir crest
 S
           top width of the water surface
 \mathbf{T}
           mean velocity at any point
 V
           upstream mean velocity
 V_4
Vc
           critical velocity corresponding to upstream flow
           velocity of the jet
           distance along the side-weir measured from upstream
 \mathbf{x}
           end of the weir
```

y	depth at any point			
y <sub>1</sub>	upstream depth measured at the centre line of the			
	channel			
y <sub>2</sub>	downstream depth measured at the centre line of the			
	channel			
Уc	critical depth corresponding to upstream flow			
y <sub>n</sub>	normal depth in the upstream channel			
Z	section factor			
z	height of the bed of the channel above a datum			
α	energy coefficient			
β	momentum coefficient			
θ	angle of the jet			
<b>9</b> •	inclination of the jump front with to the centre			
	line of the channel			
Ø	varied flow function			

### ABSTRACT

An extensive experimental study has been done on the behaviour of side-weirs in the rectangular channels. The spatially varied flow equation of De Marchi for the flow along the side-weir has been found to be useful for the determination of discharge over the side-weirs. The parameters affecting the coefficient of discharge have been identified. In subcritical flow, an expression has been derived analytically for the variation of the discharge coefficient of a side-weir of zero height with the Froude number of upstream main flow. The experimental data show a very good agreement with this expression. In supercritical flow the discharge coefficient is virtually independent of any of the flow parameters. The discharge coefficient of side-weirs of finite height has been studied experimentally and is shown to be essentially the same as for the corresponding side-weir of zero height.

An empirical equation similar to ordinary weir formula has been developed for easy solution of discharge over the sideweirs and has been found to give the accuracy of  $\pm$  10% upto upstream Froude number of 0.5.

The hydraulic jump occurring along the side-weir has been studied in an exploratory way.

#### CHAPTER T

#### INT RODUCTION

A side-weir is defined as a free overflow weir set into the side of a channel with the purpose of allowing part of the liquid to spill over the side if the surface of the flow in the channel rose above the side-weir crest. It is also called as side-spillway or lateral spillway. As contrary to the function of ordinary weir which blocks up the flow in the main channel, the function of a side-weir is to facilitate the overflow.

Some of the situations in hydraulic engineering where side-weirs are in use are:

- a) In sanitary engineering practice the side-weir is used extensively as stormflow outlet in the combined sewer system, to pass a chosen proportion of the storm water to some convenient river, stream or estuary, at the earliest possible moment so as to reduce the cost of the sewer system.
- b) In an irrigation canal system the surface runoff may sometimes be let into a canal and excess flow may be disposed off at some convenient location downstream to some other canal, river, stream or estuary. The various structures which could be used for this purpose are (1) Bottom-rack (11) sluice gate set into the

- side (1ii) side-weir. Both the bottom-rack and the sluice gate have been mainly used as sediment extractors. In case the interest lies in passing out top layers of the main flow having less sediment content, provision of a side-weir will be advantageous.
- embankments from overtopping at the time of floods.
- d) In the hilly regions the intake of the diversion canals may be situated in a deep and narrow gorge. Circumstances may require provision of a side-weir in the head works. Such was the situation in the case of head works of the Ouse-Great Lake canal taking off from Ouse-river in U.S.A. (8).
- e) A branch canal or distributory at its take-off point usually has a sluice gate fixed over a sill for the control of the discharge. When the sluice gate is fully lifted, water spills over freely and in such a case the structure should be recognised as a free overflow side-weir. The discharge into the tributory in such a case will be as a result of side-weir action.
- f) Water from gutters of residential streets is sometimes diverted to subsurface drains by means of kerb-opening inlets. When the slot inlet is partially submerged, the structure should be recognised as a free over flow side-weir set into the side of a channel of triangular cross-section.

g) In the recent years side-weir has also found some use in thermal power installations. After cooling the power plant, sometimes the warm water is carried in a channel to be spread over a long length of the pond with the use of a side-weir.

Fig. 1.1 is a definition sketch in which various parameters appearing in the side-weir problem have been defined. For the known initial flow  $({}^{\cdot v}_{1}, v_{1})$  and the geometry of side-weir (L, B, S), the problem of side-weir consists of:

- i) prediction of discharge division  $(Q_s/Q_1)$ , and
- ii) prediction of water surface in the vicinity of the sideweir.

Till year 1928 there existed a few empirical formulae for calculating the flow over a side-weir. A theoretical approach to the problem was given by Nimmo (8) in year 1928 and DeMarchi(3) in the year 1932. For spatially varied flow with withdrawal of water from sides and with certain assumptions regarding specific energy (E) and weir action DeMarchi derived the following equation for the variation of depth along the side-weir in rectangular channel (3).

$$x = \frac{3}{2} \frac{B}{C_M} \left[ \phi \left( \frac{y}{E} \right) + k \right] \qquad \dots (1.1)$$

where

$$\emptyset(\frac{y}{E}) = \frac{2E-3s}{E-s} \sqrt{\frac{E-y}{y-s}} - 3 \sin^{-1} \sqrt{\frac{E-y}{E-s}} \dots (1.2)$$

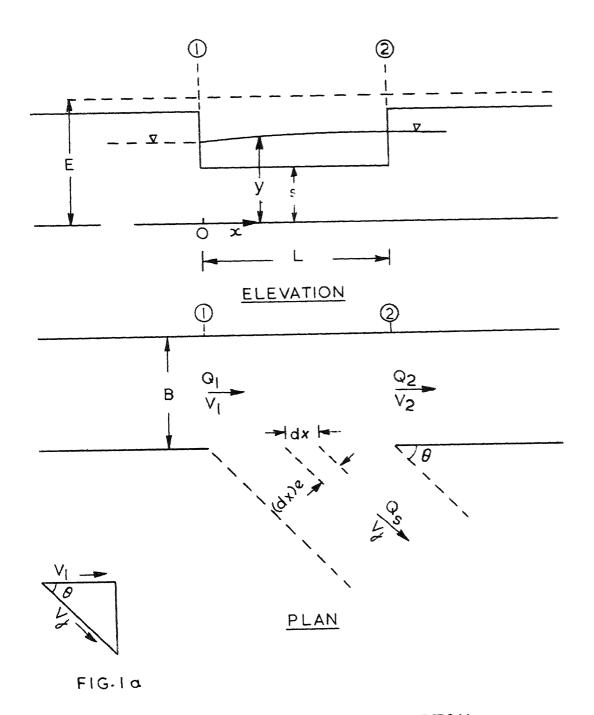


FIG. 1.1 DEFINITION SKETCH

 $E = y + \frac{v^2}{2g} = \text{specific energy, constant along}$  the weir

x = distance along the weir

y = depth of water at any point

V = mean velocity at any point in x direction

s = height of weir crest above channel bottom

C<sub>M</sub>, k are constants

B = width of the channel

g = acceleration due to gravity (Ref. Fig. 1.1)

Further in the year 1957 there were a few exploratory works which were either not much different from the previous works or empirical in nature.

The present state of knowledge on side-weirs is insufficient to explain fully the mechanics of flow. Even though it is found that DeMarchi theory could be satisfactorily applied for predicting the flow profile and the discharge division, the knowledge about the behaviour of the experimental coefficient  $(C_M)$  is lacking.

The present investigation was undertaken with the following objectives:

- 1) to have a better understanding of the flow mechanism.
- 1i) to study the variation of the coefficient of discharge  $(C_M)$  with other parameters of the problem.
- 111) to predict the discharge division  $(Q_s/Q_1)$ , if possible, by a simpler procedure.

The details of the investigation have been presented in Chapters III, IV, and V. A detailed study of the existing literature which formed a basis for present study is presented in the next chapter.

### CHAPTER II

### LITERATURE REVIEW

It appears that the pioneering work on the problem of side—weirs has been done in the field of public health engineering in the early years of 20th century. Since then this problem has attracted the attention of many investigators who have evolved various theories and formulae giving the relationships between quantity, depths of flow and lengths of side—weirs. A brief review of the some of the empirical formulae has been presented in table I.

A rational approach to the problem of side-weirs was given by DeMarchi (3) in year 1932, based on following assumptions:

- a) The flow is unidirectional
- b) The velocity distribution across the channel section is constant and uniform; that is, the velocity distribution coefficients are taken as unity. However, proper values of the coefficients may be introduced, if necessary.
- c) The pressure in the flow is hydrostatic; that is, pressure distribution coefficients are taken as unity.
- d) The slope of the channel is relatively small, so its effects on the pressure head and on the force on the channel sections are negligible.

Table I: Existing Empirical Formulae

Sl.	Authors	Ro <b>f</b> e en <b>c</b> e	H' <b>O</b> PIMIL DO	Units	Remarks
1.	Engels	6	Q <sub>s</sub> =3.32L· <sup>83</sup> (y <sub>2</sub> -s) <sup>1.67</sup>	F.P.S.	Large scale model. not useful for design
			$Q_s = 3.32L^{9} (y_2 = s)^{1.60}$	F.P.S.	Width gradually reduced
2.	Fruhling		$Q_s = 4 L h_1^{1.5}$	F.P.S.	Gives high dis- charge
3.	Parmley	4	$L = \frac{B_{W}V}{1.67} \left( \sqrt{\frac{1}{h_{2}}} - \sqrt{\frac{1}{h_{1}}} \right)$	F.P.S.	For h <sub>2</sub> =0, L is ∞ ,
			۷ ۱		Always falling
š					profile
4.	Coleman and				
	Smith	4	L=29.06 B <sup>1.4</sup> n <sup>0.513</sup>		,
		f	Q <sub>S</sub> =1.674 BL. 72h1.645	F.P.S.	Always falling
		ı	***		profile
5.	Babbit	6	$L=2.3V_1.D.Log_{10}(\frac{y_1-s}{y_2-s})$	F.P.S.	Always falling
			2		profile
					· ·

Where,

D = diameter of the pipe

 $V_1$  = upstream velocity

h, = upstream depth over the weir

 $\mathbf{B}_{\mathbf{w}} = \mathbf{w} \cdot \mathbf{d} \mathbf{t} \mathbf{h}$  at the weir level

V = velocity at any point along the weir.

e) The flow may be treated as flow diversion where the diverted water does not affect the energy head, i.e. the specific energy along the side-weir is constant; that is,

$$E = y + \frac{v^2}{2g} = \text{specific energy, constant along the}$$
  
side-weir ... (2.1)

where, y, V are depth and mean velocity at any cross-section.

f) The ordinary weir formula

$$q_s = \frac{2}{3} c_M \sqrt{2g} (y-s)^{3/2} \dots (2.2)$$

is applicable, where

 $C_{M} = a discharge coefficient$ 

s = the height of the weir crest.

The total energy (H) at a channel section is given by:

$$H = z + y + \alpha Q^2 / 2gA^2 \qquad ... \qquad (2.3)$$

\*where, Q = discharge through any cross section along the weir

z = distance of the bottom of the channel section above a horizontal datum.

A = Area of the flow section

Differentiating equation (2.3) with respect to x,

$$\frac{dH}{d\mathbf{x}} = \frac{dz}{dx} + \frac{dy}{dx} + \frac{\alpha}{2g} \left( \frac{2Q}{A^2} \frac{dQ}{dx} - \frac{2Q^2}{A^3} \frac{dA}{dx} \right) \qquad \dots \qquad (2.4)$$

and noting that  $\frac{dH}{dx} = -S_f$ ,  $\frac{dz}{dx} = -S_o$ ,  $\frac{dQ}{dx} = q^*$ ,

$$\frac{dA}{dx} = \left(\frac{dA}{dy}\right)\left(\frac{dy}{dx}\right) = T \frac{dy}{dx}$$

the equation (2.4) is reduced to

$$\frac{\mathrm{dy}}{\mathrm{dx}} = \frac{\mathrm{S_0 - S_f} - \alpha \mathrm{Qq}^* / \mathrm{gA}^2}{1 - \alpha \mathrm{Q}^2 / \mathrm{gA}^2 \mathrm{D}} \qquad \dots \qquad (2.5)$$

where D = A/T

Equation (2.5) is the dynamic equation for spatially varied flow with decreasing discharge.

Since the specific energy (E) along the side-weir is assumed constant, i.e.  $S_f = S_o$  and for horizontal channel  $S_o = 0$ , taking  $\alpha = 1.0$ , for rectangular channel equation (2.5) is reduced to:

$$\frac{dy}{dx} = \frac{Qy \left(-dQ/dx\right)}{gB^2y^3 - Q^2} \qquad ... \qquad (2.6)$$

$$-\frac{dQ}{dx} = q_s = \frac{2}{3} C_M \sqrt{2g} (y-s)^{3/2} \dots (2.7)$$

From equation (2.1)

$$Q = By \sqrt{2g(E-y)} \qquad ... \qquad (2.8)$$

From equations (2.6, 2.7 and 2.8,)

$$\frac{dy}{dx} = \frac{4}{3} \cdot \frac{C_{M}}{B} \frac{\sqrt{(E-y)(y-s)^{3}}}{3y-2E} \qquad ... \qquad (2.9)$$

On integrating,

$$x = \frac{3}{2} \cdot \frac{B}{C_M} \not D \left(\frac{y}{E}\right) + constant \qquad ... \qquad (2.10)$$

where

$$\emptyset \left( \frac{y}{E} \right) = \frac{2E - 3s}{E - s} \sqrt{\frac{E - y}{y - s}} - 3 \sin^{-1} \sqrt{\frac{E - y}{E - s}} \dots$$
 (2.11)

 $\emptyset$  (y/E) is a varied flow function.

For a side-weir of length L,

$$L = \frac{3}{2} \frac{B}{C_{M}} (\emptyset_{2} - \emptyset_{1}) \qquad ... \qquad (2.12)$$

where suffix 1 and 2 refer to beginning and end of the weir.

Collinge (5) plotted DeMarchi function  $\emptyset(y/E)$  against y/E for different values of s/E for easy solution of equation (2.12). He found experimentally that the discharge coefficient ( $C_M$ ) decreases with increase in mean velocity along the weir.

Ackers (1) derived an equation which is similar to DeMarchi equation. He considered the momentum and energy coefficients which were considered to be unity by DeMarchi, and obtained

$$L = \frac{B}{C} \sqrt{2g/\alpha} \left[ \left\{ (2 - \frac{\beta s}{E_w}) \left( \sqrt{\frac{E_w}{h_2} - \beta} - \sqrt{\frac{E_w}{h_1} - \beta} \right) \right\} - \left\{ 3\sqrt{\beta} \left( \cos^{-1} \sqrt{\frac{\beta h_2}{E_w}} - \cos^{-1} \sqrt{\frac{\beta h_1}{E_w}} \right) \right\} \right] \qquad (2.13)$$

where,

$$E_{W} = h + \frac{v^2}{2g} = constant$$

h = depth above the weir crest

 $\alpha$  = Energy coefficient

β = momentum coefficient

h<sub>1</sub> = upstream depth above the weir crest

 $h_2$  = downstream depth above the weir crest

As a result of experimental investigations he found that  $\alpha = 1.4$ ,  $\beta = .8$ , C = 3.33 (f.p.s. units) and  $h_1 = \frac{1}{2} E_w$ 

For the special case in which h<sub>2</sub> is taken as 1.9 cms (1/16 ft.), he derived a simplified equation for the design of the side-weir.

$$L = 2.03 B (5.28 - \frac{2.63 s}{E_W})$$
 in f.p.s. units (2.14)

This formula was stated to be applicable for the case of falling profile which he found would occur if s/E  $_{\!_W}$  < 1.

It should be noted here that the reliable information on the value of  $C_M$  corresponding to various flow conditions is lacking. Ackers (1) suggests a value of  $C_M = 0.625$  if y is measured at a remote distance from the plane of the weir and  $C_M = 0.725$  if y is measured at the plane of the weir. Apparently  $C_M$  is assumed to be constant by him. Collinge (5) finds that  $C_M$  varies with the mean velocity of the main channel.

Allen (2) in connection with his work on side-weirs in circular pipes found that:

$$\frac{Q_{\rm S}}{Q_{\rm a}} = C_{\rm a} (L/D)^{2/3}$$
 ... (2.15)

where

$$C_a = 0.22 \text{ D/B}_w \text{ (empirical)}$$

 $B_{w}$  = width of the water surface at weir level

 $Q_a = available flow$ 

(The flow corresponding to the depth equal to sill height is not available for flow over the weir. Unavailable flow subtracted from total flow gives the available flow.)

Frazer's(6) approach to the problem is simple semiempirical curve fitting. He derived correlation equations for following cases:

(i) Rapid Flow: Correlation of quantity and depth of flow

$$q_r = y_r \sqrt{2.5 - 1.5 y_r}$$
 ... (2.16)

where

$$q_r = Q/Q_1$$

$$y_r = y/y_c$$

 $y_c$  = critical depth corresponding to initial flow

(ii) Rapid flow: Correlation of quantity and length

$$q_{\infty} = C_r \sqrt{2.5 - 1.5 C_r}$$
 ... (2.17)

where

 $q_{\infty} = discharge$  in the downstream channel

$$C_r = s/y_c$$

$$\frac{1-q_r}{1-q_m} = 1 - 10^{-L/8B} \qquad ... \qquad (2.18)$$

The left hand side is the ratio of the discharge over the weir in the length  $l=L/y_c$  to the discharge over a weir of the same proportionate height whose length is infinite.

(iii) Subcritical Flow: Correlation of quantity and depth of flow:

$$q_r = y_r \sqrt{0.99 \theta_1 - 2y_r}$$
 ... (2.19)

where,

$$\theta_1 = 2y_{1,r} + \frac{1}{(y_{1,r})^2}$$

$$y_{1,r} = y_1/y_c$$

(iv) Subcritical Flow: Correlation of quantity and length

$$Q_{1} - Q_{2} = \frac{2}{3} C_{b} \sqrt{2g} (\bar{y} - s)^{1.5} L \qquad ... \qquad (2.20)$$

$$1 - Q_{2} = C_{II} (\bar{y}_{r} - s_{r})^{1.5} . x_{r}$$

where,

or

$$q_2 = Q_2/Q_1$$
 $x_r = L/B$ 
 $\overline{y}_r = (2y_2, r + y_1, r)/3$ 
 $y_2, r = y_2/y_c$ 

$$C_b = constant, C_{II} = \frac{2/3 \cdot C_b \cdot \sqrt{2g}}{Q_1}$$

Experimentally he found that

$$C_{II} = 0.73 - \frac{0.32}{y_{1,r}} - \frac{0.14}{1}$$
 ... (2.21)  
 $1 = L/y_c$ 

Krishnappa and Seetharamiah (7) made use of DeMarchi equation for predicting the flow in a  $90^{\circ}$  branch channel with subcritical flow in the main and supercritical flow in the branch channel. However in applying the equation they have used the heads measured directly above the weir. They found that a defined coefficient of discharge is a function of  $F_1$  and L/B, where  $F_1$  is the upstream Froude number. The experimental range both for  $F_1$  and L/B was 0 to 1. It may be noted that the analogy of side weir of zero height as a branch channel flow, used by Krishnappa and Seetharamiah (7) is not correct in view of the differences in aeration, friction and downstream confinement of flow in the two cases.

After a study of the existing literature as above the following comments could be made:

- a) The previous work is not sufficient to explain the mechanics of flow.
- the empirical formulae have dimensional constants which may be true for the experiments backing them. However, by their very nature, they cannot be of general use.

- c) Though complexity is introduced due to draw-down, splashing and non-uniformity of the flow as observed by Frazer (6), still the equation for spatially varied flow (equation 2.12) appears to be a rational and better approach to the problem.
- d) The reliable information on the coefficient of discharge ( $G_M$ ) is lacking.
- e) A cross section of the channel will show a H<sub>2</sub> type water surface profile. In applying DeMarchi equation (2.12) the selection of the right depth is a problem. Use of depth over the weir, as done by Krishnappa and Seetharamiah (7) is not a happy choice, as the depth over the weir suffers from the defects of (a) curvature of the from stream lines (b) the pressure is different than hydrostatic. Probably the centre line depth will be a better depth to use.

Chapter III deals with the experimental details of the investigation which was carried out with a view to improve the existing state of knowledge on side-weirs.

#### CHAPTER III

### EXPERIMENTS

### 3.1 Introduction

An experimental study of the problem of side-weir in a prismatic horizontal rectangular channel was carried out at the hydrau-licslaboratory of the Indian Institute of Technology, Kanpur.

The justifications for the investigation were:

- a) The existing literature is insufficient.
  - (1) to explain clearly the mechanics of flow along the side-weir,
  - (1i) to predict the nature of water surface in the immediate vicinity of the side-weir.
- b) An extensive study of the variation of DeMarchi coefficient of discharge  $(C_M)$  with other parameters is lacking.
- c) DeMarchi equation is rather tedious to use in connection with side-weirs of finite height. So the investigation was also aimed at finding a simple and sufficiently reliable method of predicting discharge over side-weirs.

# 3.2 Experimental Set-up

The main experiments were conducted in a 9.0 metre long and 61 cms. wide masonary channel with horizontal bed, specially constructed for the present investigation. Using a precision level the bed of the channel was levelled accurately upto third decimal

place of a centimetre. The schematic view of the masonary channel is shown in Fig. 3.1. For furture reference this flume has been called as flume A. Verifications of some of the observations on flume A were done on a wooden flume hereafter called as flume B. Flume B was about 3 m long, 24.8 cms. wide and the bed was about 1.5 metres above the ground level. The width of the flume B was reduced to 12.4 cms. by fixing a wooden plank at the centre line of the channel in certain experiments.

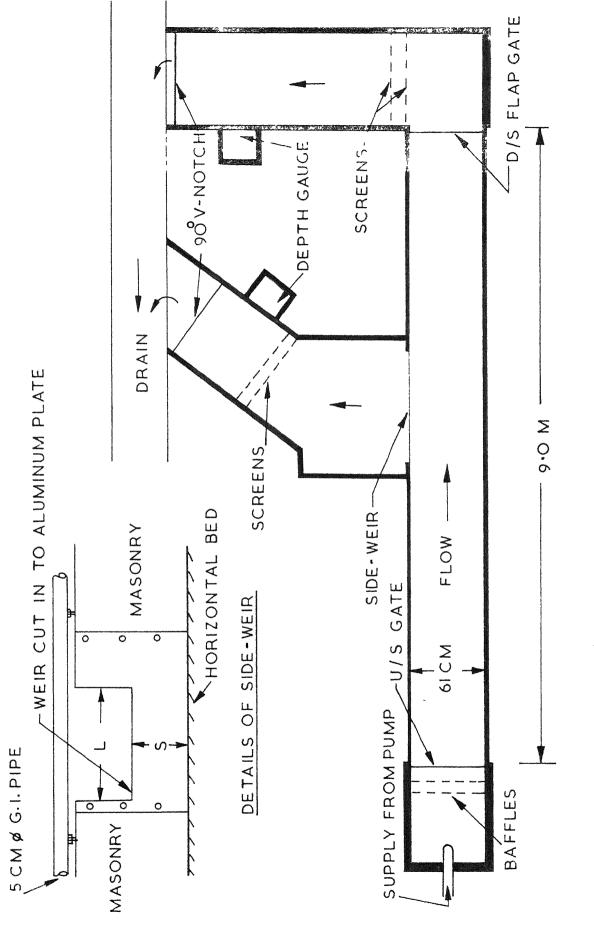
# 3.2.1 The Side-Weir

On one side of the masonary flume (flume A) a slot of ?

1 metre length was cut and an iron frame with three legs was embedded in the wall, with bottom leg being about 3 cms. below the bed of the channel. An aluminium plate was so fixed to the frame that it was flush with the inside surface of the wall. The weirs of required length and height could be conveniently cut and sharp bevelled edges made by filing. The details of a side-weir are shown in Fig. 3.1. The upstream end of the weir was fixed at 4.5 m from the upstream sluice gate. In flume B on which the studies were confined to the side-weir of zero height and subcritical flow, the side was cut and bevelled to form a weir.

# 3.2.2 The Supply

The water was fed into the channel by three pumps drawing water from under ground tank and delivering a maximum discharge of about 70 litres per second. Later the supply was doubled by connecting a supply pipe from the over head tank.



EXPERIMENTAL SET-UP SCHEMATIC VIEW OF F16.3.1

### 3.2.3 Measurements

The bed of the flume A was about 0.5 m above the ground level. Both the outgoing flow (Q2) and the flow over the weir(Qs) were received into the channels 1 m. wide. The screens were provided to make the flows uniform. The uniform flows were allowed to pass over the 90° V notches before delivering to the drain. Stilling chambers were provided for the measurement of depths over the V-notches. In the flume B where maximum supply from the pump was about 8 litres/second the flow rates were measured volumatrically. Depths in the channel were measured by point gauges accurate upto .001 ft. (.03 cms.) and fixed on an iron angle capable of being moved freely over 5 cm. dia. G.I. pipes fixed horizontal over the sides of the channel. In the flume B the velocities were measured by Prandtl type pitot tube and the readings were recorded on an inclined manometer.

After a thorough study of the existing literature it was found that a complete discription of the flow phenomenon occurring along the weir is lacking. Many runs were made for the water surface and velocity profiles along and across the side-weir. The inspection of the flow was also carried out using the dye and some sand. The study of the movement of the dye and sand particles gave knowledge about the possible places of scour and silting near the side-weir in a sandy channel.

### 3.3 <u>Water Surface Profiles</u>

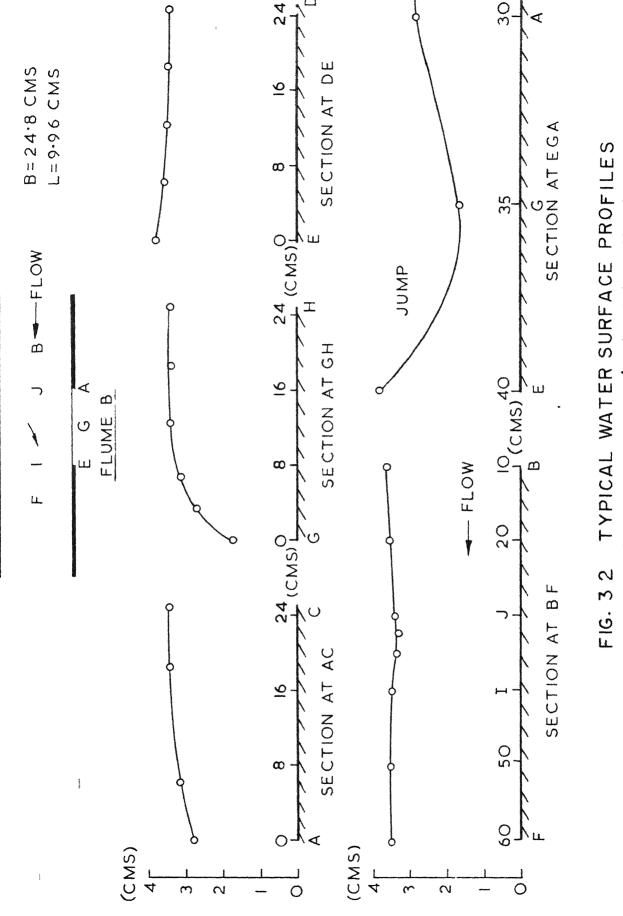
A series of runs was made with gradually increasing flows in the main channel. For each run the depth of water on the centre line was measured. The measurement of depths on the centre line was decided upon after preliminary readings had shown the effect of draw-down by the weir to be negligible at the centre line of the channel. The water surface profile at a cross-section taken across the weir was of . H<sub>2</sub> type. The typical water surface profiles have been shown in Fig. 3.2. It could be seen that the depth profile in the plane of the weir is highly uneven. Any formula based on depth measurements over the weir should be expected to give considerable errors.

# 3.4 The Velocity Profiles

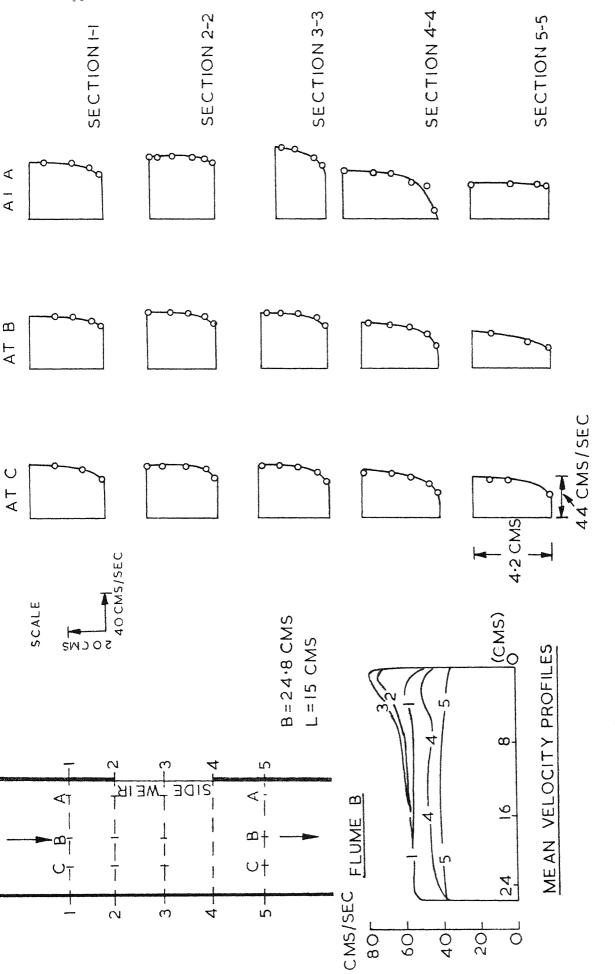
The typical velocity profiles have been shown in Fig. 3.3. It will be seen from the plot of mean velocity that the side-weir affects the flow conditions considerably upstream. The approaching uniform flow gets accelerated when it reaches near the upstream end of the weir. The energy coefficient  $\alpha$ , is of the order of 1.03 and momentum coefficient  $\beta$  is approximately 1.01. But while applying the DeMarchi equation the error due to object of  $\alpha$  and  $\beta$  may be negligible.

# 3.5 Flow Separation

A problem with the normal outlet like side-weir lies in the possibility of flow separation which results in unfavourable



(Expt. no.8-38) (Subcritical flow)



TYPICAL VELOCITY PROFILES (Expt.no. B-45B) (Subcritical flow) FIG. 3.3

pressure gradients and 'distortion of velocity profiles. The flow coming out of the channel produces a suction effect, as a result the stream lines are curved towards the side-weir. There is tendency of flow separation on the side of channel opposite to the side-weir. The location of the separation depends on

- a) the quantity of flow passing over the weir,
- b) the velocity in the channel
- c) the length of the weir. Once the separation occurs a pocket of back flow is formed which extends further into down-stream channel. The size of the back flow pocket is bigger with low Froude numbers. The observations have shown that in case of weirs of finite height the point just downstream end of the weir is susceptible to flow separation, as the flow at that point seems to move up trying to separate from the bed. In case of channels with sandy bed, provision of a smooth transition in the width may possibly solve the problem of silting resulting due to formation of back flow pocket.

# 3.6 Discharge Division

The efficiency of the side-weir may be defined as the ratio of the flow over the weir to the upstream discharge, i.e.  $Q_s/Q_1$ . A total of 200 experiments belonging to 10 series were conducted to study the efficiency of the side-weirs. The corresponding data have been presented in appendix A. The range of

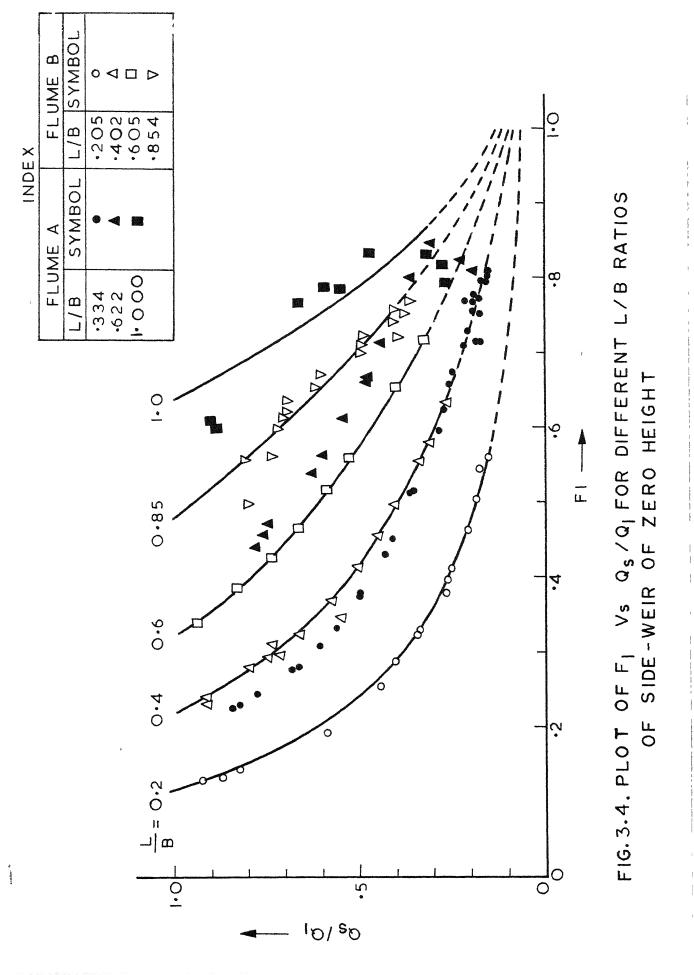
Various parameters studied are shown in Table II.

Table II: Range of Parameters Studied

Parameter	Range
F <sub>1</sub>	0.02 - 4.3
L/B	0.2 - 1.0
s/y <sub>1</sub>	0.2 - 0.96
y <sub>1</sub> /L	0.1 - 2.4

For the weirs of zero height the efficiency of the weir for different L/B ratios has been plotted against upstream Froude number (F<sub>1</sub>) in Fig. 3.4. The efficiency of the side-weir ( $Q_{\rm S}/Q_1$ ) decreases with increase in Froude number (F<sub>1</sub>).

The further analysis of the data has been presented in Chapters IV and V.



#### ANALYSIS

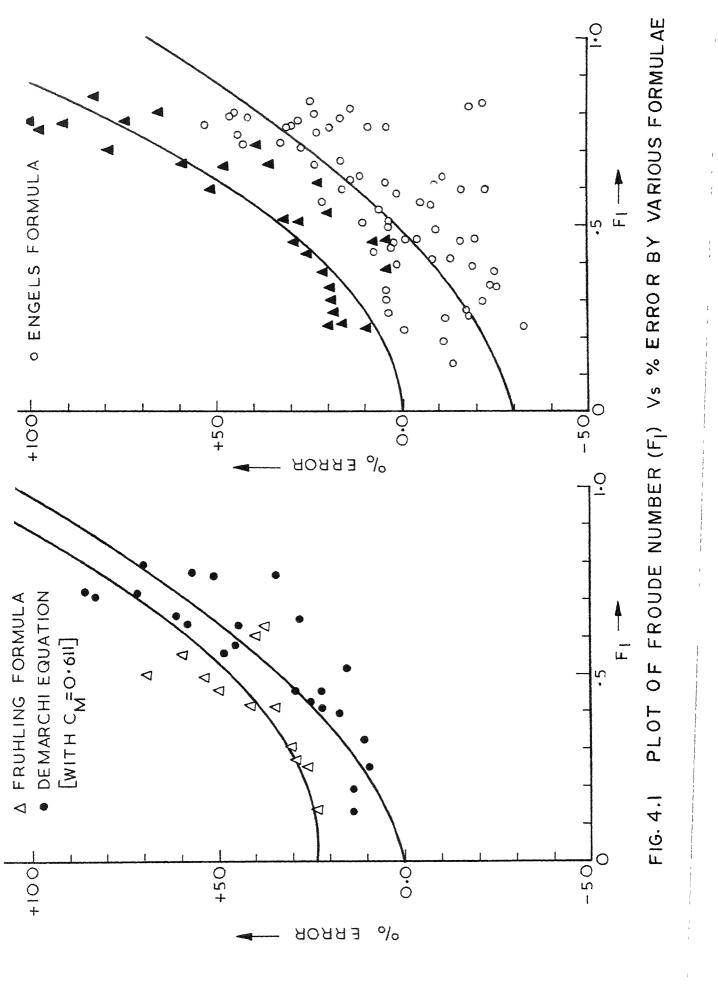
#### 4.1 Existing Formulae

In the first stage of the analysis of the experimental dat it was found necessary to ascertain the validity and applicabilit of the existing formulae. In Fig. 4.1 the percentage error given by some of the well known existing formulae is plotted against th upstream Froude number  $(F_1)$ . It will be seen that the percentage error increases with increase in the upstream Froude number  $F_1$ . It should be noted that the value of the discharge coefficient  $(C_M)$  in DeMarchi equation was assumed constant and equal to .611, due to lack of information. In the other formulae the depth should probably be measured over the weir. But in the calculation of percentage error centre line depths were used. However, it is quite clear that the discharge division is function of the upstre Froude number. Any formula giving discharge over the side-weir should have upstream Froude number as dominant parameter.

#### 4.2 De Marchi Equation

It was concluded in Chapter II that the best rational approach to the problem seems to be that which is given by De Marchi, Writing here again the De Marchi equation (2.12)

$$L = \frac{3}{2} \frac{B}{C_{M}} (\emptyset_{2} - \emptyset_{1}) \qquad \dots \qquad (4.1)$$



where suffix -1 and 2 refer to beginning and end of the weir. If conditions at section 1 (ref. Fig. 1.1) are known (i.e.  $Q_1$ ,  $y_1$ )  $\emptyset_2$  and hence  $Q_2$  and  $y_2$  can be found, provided  $C_M$  is known. The total discharge over the side-weir,  $Q_8$  would then be

$$Q_{s} = Q_{1} - Q_{2} \qquad \dots \qquad (4.2)$$

# 4.3 De Marchi Coefficient, C<sub>M</sub>

It was observed in Chapter II that reliable information on the value of  $\mathbf{C}_{\mathbf{M}}$  corresponding to various flow conditions is lacking. It is needed to analyse its behaviour based on some theoretical reasoning.

Dimensional analysis indicates that

$$C_{M} = fm. (F_{1} = \frac{V_{1}}{\sqrt{gy_{1}}}, \frac{L}{B}, \frac{y_{1}}{L}, \frac{s}{y_{1}})$$
 (4.3)

It should be expected that  $F_1$  would be a significant parameter affecting the value of  $C_{\overline{M}}$  and the remaining parameters, representing the geometrical configuration would be having small effects, if any.

For a side-weir of zero height (i.e. s = 0).

$$C_{M} = fn \quad (F_{1}, \frac{L}{B}, \frac{y_{1}}{L}) \qquad \dots$$
 (4.1)

Assuming L/B and y<sub>1</sub>/L have very insignificant effect, an expression for the variation of  $C_{\mathbb{M}}$  with  $F_1$ , for a weir of zero height is derived as follows.

# 4.4 Variation of $C_{\overline{M}}$ with $F_1$ for Side-Weir of Zero Height

The flow over the side-weir can be considered as a deflected jet, as in Fig. 1.1. Consider an elemental length dx of the weir. According to equation (2.2)

$$Q_s = qs \cdot dx = \frac{2}{3} C_M \sqrt{2g} dx \cdot y^{3/2}$$
(\*. s = 0) ... (4.5)

Since the effective width of the jet through this element is reduced such that  $(dx)_e = dx$ . Sin  $\theta$  the discharge  $Q_s'$  can be rewritten as

$$Q_s' = \frac{2}{3} C_M^* \sqrt{2g} dx \sin \theta y^{3/2}$$
 (4.6)

where  $C_{\mathbb{M}}^{\phantom{M}}$  is a constant coefficient. Also, as a first approximation, in subcritical flow

Sin 
$$\theta = \sqrt{1 - (v_1/v_j)^2}$$
 ... (4.7)

Now it is assumed that the critical depth corresponding to occurs at the plane of the side-weir of zero height such that q s

$$\frac{V_c^2}{2g} = \frac{1}{3} E$$
 ... (4.8)

$$E = y_1 + \frac{{v_1}^2}{2g} \qquad (4.9)$$

where 
$$E = y_1 + \frac{1}{2g}$$
  
substituting  $V_c = V_j$  and noting  $F_1^2 = \frac{V_1^2}{gy_1}$ 

$$\sin \theta = \sqrt{1 - \frac{3F_1^2}{F_1^2 + 2}}$$
 (4.10)

where  $C_{\mathbb{M}}^{\times}$  can be assumed to be 0.511 as it represents the efflux from a constriction with  $F_1 \to 0$ , with this

$$C_{M} = 0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2} + 2}}$$
 ... (4.11)

Eqn. 4.11 could be expected to give the variation of  $C_{\rm M}$  with  $F_1$  for subcritical flow over a side-weir of zero height.

In supercritical flow, however, the discharge coefficient  $\mathbf{C}_{\mathbb{M}}$  could be assumed to be essentially independent of the Froude number as the zone of influence of the side-weir will be confined to its immediate neighbourhood only.

#### 4.5 Experimental Study:

a) Subcritical Flow: Fig. 4.2 shows a plot of  $C_M$ , calculated from experimental data for side-weirs of zero height, plotted against the upstream Froude number of the flow. Only data for subcritical region is shown in this plot. Also plotted are the variation of  $C_M$  given by Eq. 4.11. It can be seen that all the plotted points follow the variation given by Eq. 4.11 very well. It can be seen that there is no effect of the parameter L/B. A further examination revealed a similar insignificant effect of the parameter  $y_1/L$ . Thus it is concluded that the expression given by Eq. 4.11 correctly predicts the variation of  $C_M$  with Froude number for subcritical flow in side-weirs of zero height.

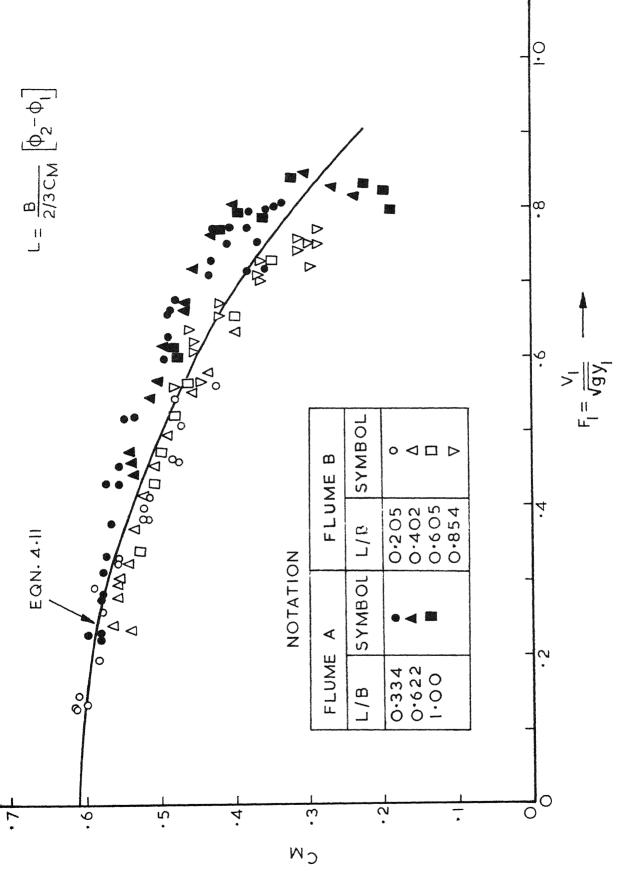


FIG. 4.2. VARIATION OF CM WITH FI FOR SIDE - WEIR OF ZERO HEIGHT

Fig. 4.3 represents the plot of the experimental data in subcritical flow over side-weirs of finite height. A very good fit of the experimental data with the line given by Eq. 4.11 is indicated. It is interesting to note the absence of any significant effect of the parameter  $s/y_1$  and also of other two parameters L/B and  $y_1/L$ . A slight observable deviation of data at a Froude number of 0.7 can be attributed to experimental errors.

b) Supercritical Flow: Fig. 4.4 shows a plot of  $C_M$  vs.  $F_1$  for supercritical flow. It is once again seen that there is an absence of the effect of the parameters L/B, s/y<sub>1</sub> and y<sub>1</sub>/L. Also the effect of Froude number  $F_1$  itself is very small, the variation being expressible as

$$C_{\rm M} = 0.36 - 0.08 \, F_{\rm 1} \, ... \, (4.12)$$

It is possible that in an ideal case  $C_{\mathrm{M}}$  would be independent of  $F_1$ . The small effect of  $F_1$ , seen in Fig. 4.4 is probably due to friction effects.

It could be concluded that the coefficient of discharge ( ${\rm C_M}$ ) in subcritical flow is necessarily a function of Froude number, given by equation 4.11 The effect of any other parameters, if any, is negligible. However,  ${\rm C_M}$  is nearly independent of Froude number or any other parameter in supercritical flow, and its value being equal to 0.36 on the average.

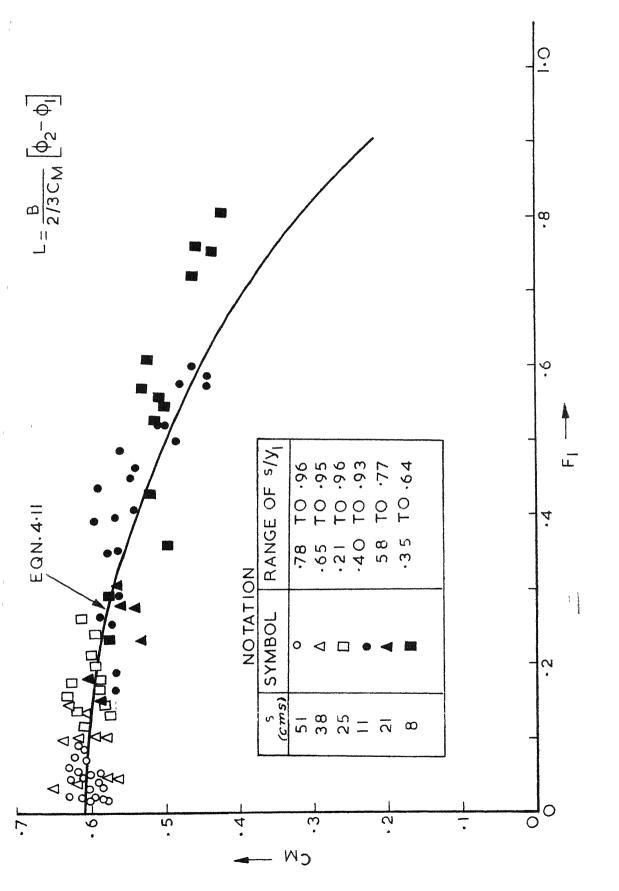
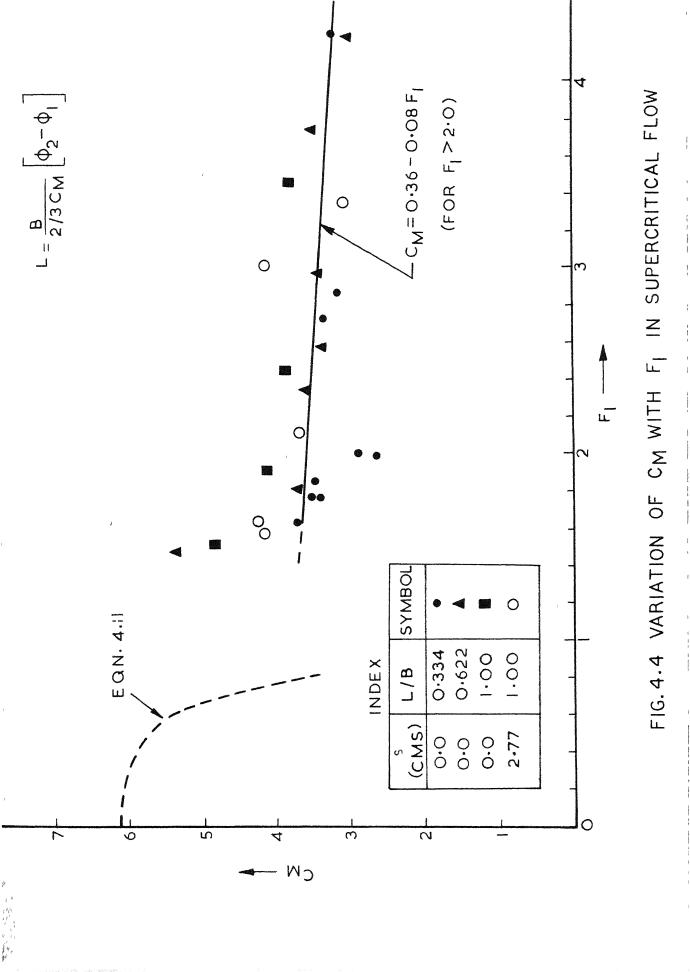


FIG. 4.3. VARIATION OF CM WITH FI FOR SIDE-WEIRS OF FINITE HEIGHT



#### CHAPTER V

#### EMPIRICAL DISCHARGE EQUATION

#### 5.1 Design Problems:

Appendix B illustrates the procedure for solving two typical design problems met in the field application of sideweir. A design chart (B-1) of varied flow function  $\emptyset$  plotted against Froude number (F) for different values of s/y ratio has been developed for easy solution of De Marchi equation, viz

$$L = \frac{3}{2} \cdot \frac{B}{C_M} (\phi_2 - \phi_1)$$
 (5.1)

The coefficient of discharge  $C_{\mathrm{M}}$  has been calculated on the basis of information presented in Chapter IV, i.e.

$$C_{M} = 0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2} + 2}}$$
 for  $F_{1} < 1.0$ 

and

$$C_{\rm M} = 0.36 - 0.08 \, F_1 \, \text{for } F_1 > 2.0$$

where  $F_1$  is already known for any design problem.

In the first type of design problem  $Q_1$ ,  $y_1$ , s are given and length L of the side-weir is to be designed for a design overflow  $Q_s$ . The procedure involves the solution of following cubic equation for  $y_2$  by trial and error.

$$E = y_2 + \frac{Q_2^2}{2g \cdot B^2 \cdot y_2^2}$$
 (5.2)

where,

$$Q_2 = Q_1 - Q_s \tag{5.3}$$

Once  $y_2$  is known,  $\phi_2$  and hence L can be calculated.

In the second type of design problem  $Q_1$ ,  $y_1$ , s, L are given and  $Q_s$  is to be found. From the given quantities and using De Marchi equation (5.1)  $\phi_2$  can be calculated. The procedure to find  $y_2$  from known  $\phi_2$  again involves a trial and error calculation which is tedious. If  $y_2$  is known  $Q_2$  (from Eqn. 5.2) and hence  $Q_s$  (from Eqn. 5.3) could be calculated.

The labour involved in trial and error procedure could be reduced  $\mathfrak{t}$ f  $Q_s$  could be calculated approximately by some other method, say by empirical formula.

#### 5.2 Empirical Formula:

It would be very convenient to calculate  $Q_s$ , if it could be expressed by a simple discharge formula involving L,  $y_1$ , and s. With this in view,  $Q_s$  is expressed by the following Eq.(5.4) which is very similar to ordinary weir formula:

$$Q_s = C_d \frac{2}{3} \sqrt{2g} \cdot L \cdot (y_1 - s)^{3/2}$$
 (5.4)

in which  $\mathbf{C}_{\mathbf{d}}$  is a coefficient which takes into account the,

- a) curvature effect of the stream-lines
- b) velocity and pressure distribution
- c) approaching velocity head
- d) side contractions
- e) variation of depth along the weir.

Dimensional analysis indicates that

$$C_d = Fn \quad (F_1 = \frac{V_1}{Vgy_1}, \frac{L}{B}, \frac{h_1}{L}, \frac{s}{y_1})$$

$$... (5.5)$$
 $h_1 = (y_1 - s)$ 

where

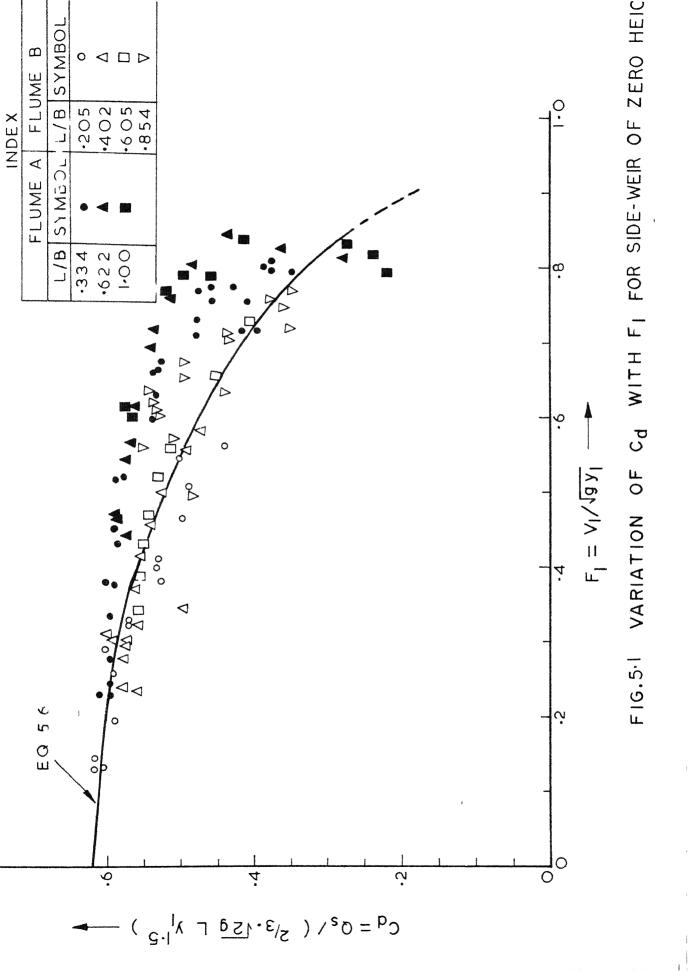
#### 5.2.1 Subcritical Flow:

By arguments similar to the one proposed for the variation of  $C_{\rm M}$  in section 4.4, it could be shown that for small values of  $y_1/L$ , L/B and s/y = 0,

$$C_d = f_1(F_1) = 0.611 \sqrt{1 - \frac{3F_1^2}{F_1^2 + 2}}$$
  
in subcritical flow (5.6)

However, for finite values of  $s/y_1$  and large values of L/B and  $y_1/L$ , the effect of these parameters on  $C_d$  could be expected to be significant.

Figs. 5.1 and 5.2 show the variation of  $C_d$  with  $F_1$  in subcritical flow for weirs of zero height and for weirs of finite height. The equation (5.6) is also shown plotted in these figures. The close examination of the plotted points revealed that the scatter in these figures is mainly due to the effect of the parameter  $h_1/L$ . The effect of other parameters L/B and s/y<sub>1</sub> is not very apparent.



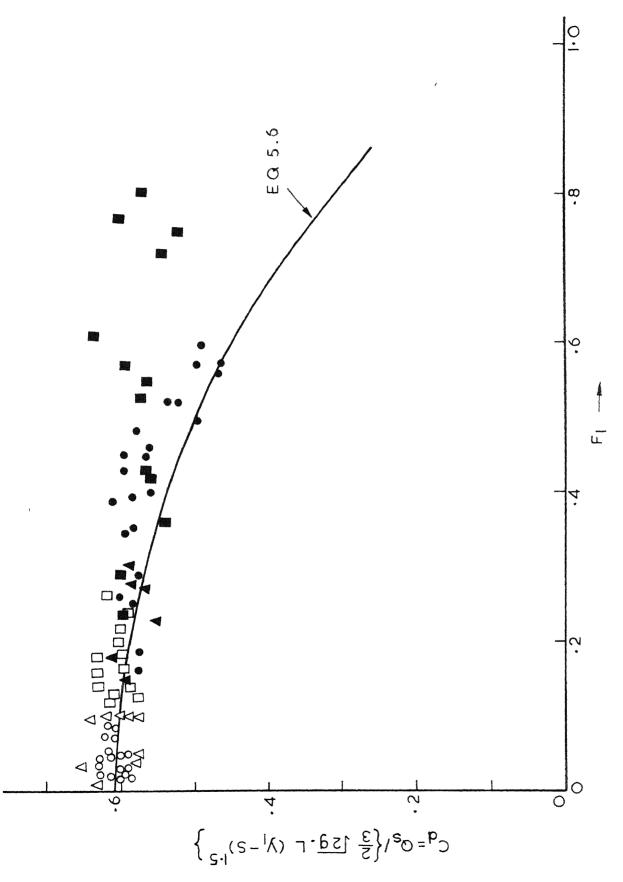


FIG. 5.2. VARIATION OF Cd WITH FI FOR FINITE HEIGHT OF WEIRS

The variation of  $C_d$  for subcritical flow is expressed as

$$c_{d} = f_{1}(F_{1}) \left(\frac{h_{1}}{L}\right)^{p} \left(\frac{L}{B}\right)^{q} \left(\frac{s}{y_{1}}\right)^{r} \dots (5.7)$$
or
$$f_{1}(F_{1}) = 0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2} + 2}} = \frac{c_{d}}{(h_{1}/L)^{p}(L/B)^{q}(s/y_{1})^{r}} \dots (5.8)$$

From the experimental data for weirs of zero height as well as for weirs of finite height values of p,q,r which gave least variance from the curve of  $C_d = f_1(F_1)$  (Eqn. 5.6) were found with the aid of digital computer. It was found that the effect of the parameters L/B and  $s/y_1$  were insignificant (i.e. q = 0, r = 0). The value of p was found to be 0.06. Hence the discharge equation in subcritical flow could be taken as

where
$$C_{d} = C_{d} \cdot \frac{2}{3} \sqrt{2g} \cdot L (y_{1}-s)^{3/2}$$

$$C_{d} = (0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2}+2}}) \times (\frac{y_{1}-s}{L})^{.06} .(5.9)$$

The formula (5.9) though empirical has the advantage of simplicity. From this approximate value of  $\mathbf{Q}_{\mathbf{S}}$  can be calculated very easily. It is necessary to verify this formula (5.9) with the experimental results to ascertain the amount and nature of the error. It could be expected that the error in the calculation of  $\mathbf{Q}_{\mathbf{S}}$  ( %Error) will be more with high Froude numbers. The

percentage error has been plotted against upstream Froude number  $(F_1)$  in Fig. 5.3. It could be seen that the error is within  $\pm$  10% band upto  $F_1$  = 0.55 (only 9 out of 98 points fall slightly out of this band). For higher Froude numbers the error is large. This could possibly be **due** to the experimental errors as at high Froude numbers the depth was small **and** water surface was wavy.

It is concluded that equation (5.9) may be used for the approximate estimate of side-weir discharge for small. Froude numbers, (i.e.  $F_1$  < 0.5) with the accuracy of  $\pm$  10%.

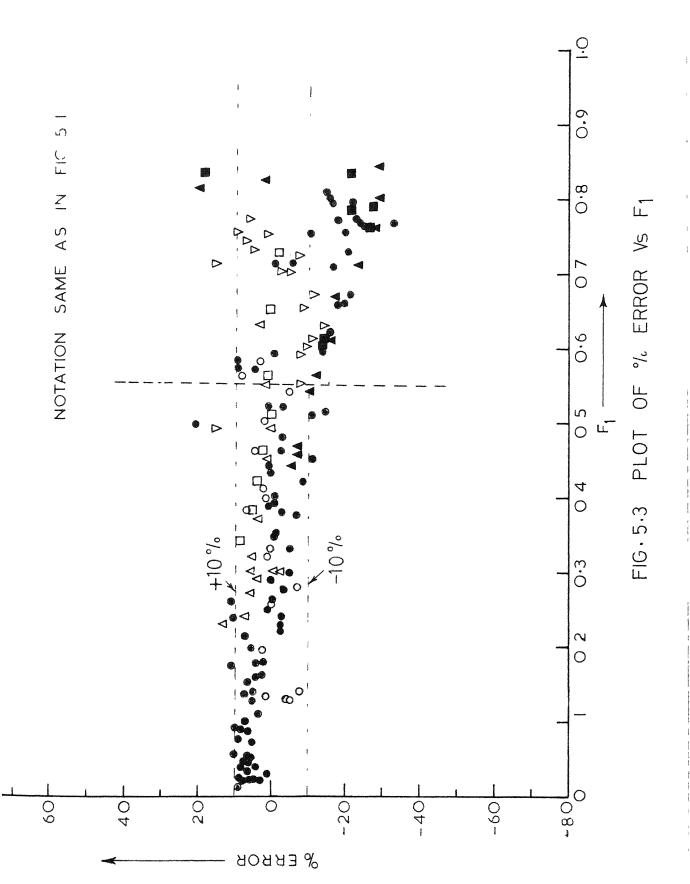
#### 5.2.2 Supercritical Flow:

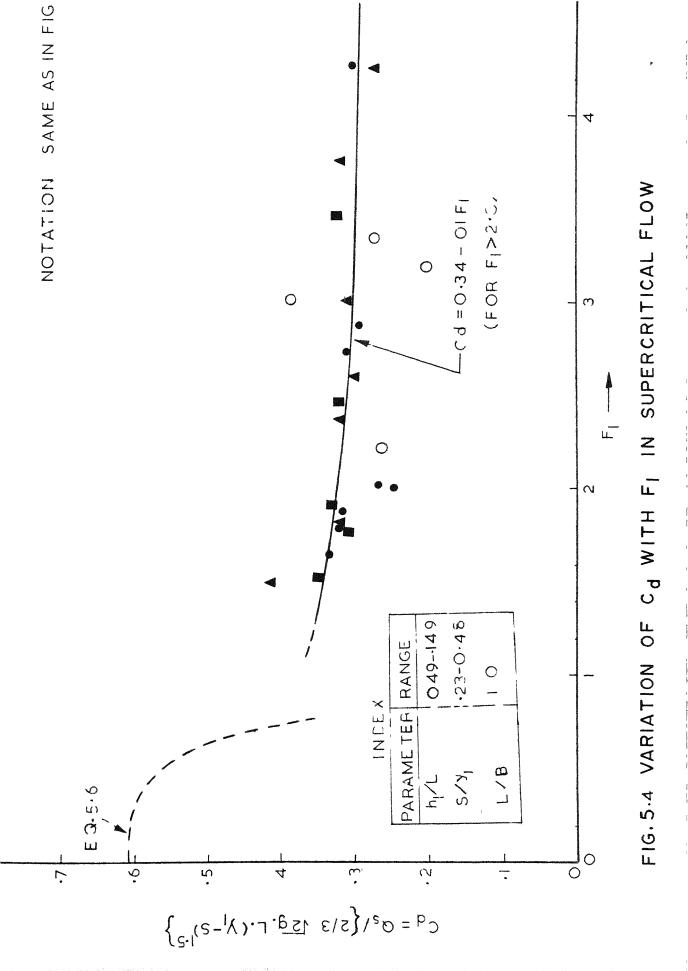
It was observed in section 4.5(b) that the coefficient of discharge  $C_{\rm M}$  is virtually independent of upstream Froude number  $(F_1)$ . Like  $C_{\rm M}$ , coefficient  $C_{\rm d}$  should also be expected to be independent of  $F_1$ , i.e. fairly constant in supercritical regime.

Fig. 5.4 shows the variation of  $\mathbf{C}_{d}$  with  $\mathbf{F}_{1}$  in supercritical flow. The data of weir of zero height closely follow a straight line variation,

$$C_d = .34 - 0.01 F_1$$
 (5.10)

showing a small effect of Froude number. Also plotted in this figure are four points for side-weir of finite height  $(s/y_1 = .23 \text{ to } .48)$ . Though there is some scatter these data





follow the line given by equation (5.10). The scatter may be attributed to the experimental errors as in these experiments the available depth over the weir was very small (of the order of 2 cms.).

It is noted that the range of parameters L/B,  $h_1/L$  and  $s/y_1$  in the supercritical flow experiments is very small to conclude any effect of these parameters on the equation (5.10). Further experimental evidence with wide range of the various parameters is needed.

#### CHAPTER VI

#### CONCLUSIONS AND RECOIDED DAITONS

#### 6.1 Conclusions

An extensive experimental study has been made on the behaviour of side-weirs in subcritical and supercritical flows. An analytical expression for the variation of De Marchi coefficient of discharge  $\mathbf{C}_{\mathrm{M}}$  has been derived. Based on the analytical as well as experimental results, the following conclusions are drawn:

- 1. The various empirical formulae for the determination of discharge over side-weirs are unsuitable for general use as they give varying degrees of error depending upon flow conditions; viz, Froude number.
- 2. De Marchi equation (2.12), which is based on logical premises could be used for discharge determination if proper discharge coefficient ( $C_{\rm M}$ ) is selected.
- The De Marchi discharge coefficient  $(C_M)$  has been found to be function of only the upstream Froude number  $(F_1)$ . The other parameters representing the geometry of the flow are found to have no effect on  $C_M$ , within the range used in the present investigation.

## (i) Subcritical Flow:

Variation of discharge coefficient  $c_{\mathrm{M}}$  is given by the equation

$$C_{M} = 0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2} + 2}}$$
 ... Eqn. (4.11)

#### (11) Supercritical Flow:

Variation of discharge coefficient  $C_{M}$  is given by the equation  $C_{M} = 0.36 - 0.08 F_{4} \qquad ... \text{Eqn. (4.12)}$ 

4. The solution of De Marchi equation (2.12) for design purposes involves tedious trial and error procedure.

An approximate formula (5.9) based on statistical correlations:

$$Q_{s} = C_{d} \cdot \frac{2}{3} \sqrt{2g} \cdot C (y_{1}-s)^{3/2}$$
where
$$C_{d} = (0.611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2}+2}}) \times (\frac{h_{1}}{L})^{.06}$$

$$h_{1} = y_{1} - s$$
(5.9)

could be used in subcritical flow for Froude numbers less than .5 with an accuracy of  $\pm$  10%.

#### 6.2 Recommendations:

1. The prediction of water surface profile in spatially varied flow along a side-weir by De Marchi equation needs to be verified by careful experimentation.

- 2. The exploratory studies on the hydraulic jump occuring along the side-weir (indicated in Appendix C) look promising. Further detailed studies are needed for the better understanding of the phenomenon.
- 3. The details of the separation zones occurring in downstream of side-weirs need to be studied.
- 4. Equation (5.9) for the determination of discharge  $Q_{\rm S}$  over a side-weir looks promising because of its simplicity. However, experiments covering wide range of different parameters (i.e.  $h_1/L$  L/B and  $s/y_1$ ) are needed to evaluate the effects of these parameters on coefficient  $C_{\rm d}$ .

#### LIST OF REFERENCES

- 1. Ackers, P, 'A Theoretical Consideration of Side-Weirs as Stormwater Overflows,' Proc. Inst. C.E. (London), Vo. 6, Feb. 1957, pp. 250.
- 2. Allen, J.W.' The Discharge of Water Over Side-Weirs in Circular Pipes,' Proc. Inst. C.E.(London), Vol. 6, pp.270-28 Feb., 1957.
- 3. Chow, V.T., 'Open Channel Hydraulics', McGraw Hill, P. 340.
- 4. Coleman, G.S. and Smith, D., 'The Discharging Capacity of Si Weirs,' Proc. Inst. C.E. (London), Selected Engineering Paper No. 6 (1923).
- 5. Collinge, V.R., 'The Discharge Capacity of Side-Weirs, 'Proc. Inst. C.E. (London), Vol. 6, pp. 288-304, Feb. 1957.
- Frazer, W., 'The Behaviour of Side-Weirs in Prismatic Rectangular Channels,' Proc. Inst. C.E. (London), Vol.6, pp. 305, Feb. 1957.
- 7. Krishnappa, G. and Seetharamiah, K., Predicting the Flow in a 900 Branch Channel with Subcritical Flow in the Main and Supercritical Flow in the Branch Channel, Symposium on Hydraulics and Hydraulic Machines, I.I.S., Bangalore (May, 1963), p. 121.
- 8. Nimmo, H.R., 'Side-spillway for Regulating Diversion Canals', Trans. Am. Soc. Civ. Engrs, Vol. 92, 1928, p. 1561

#### BIBLIOGRAPHY

- 1. Babbit, H.E., 'Sewerage and Sewage Treatment,' Willey, New York, 7th Edn. 1953.
- 2. Braine C.D.C., 'Draw-down and other Factors Relating to the Design of stormwater overflows on sewers,' J.Inst. Civ. Engrs, Vol. 28, p. 136 (Apr. 1947).
- Ven Te Chow: Discussion of Flood protection of canals by lateral spillways by Harald Tults, paper 1077, Proceeding: American Society of Civil Engineers, Journal, Hydraulics Division, vol. 83, no. HY2, pp. 47-49, April 1957.
- 4. Couloumb, R, de Saint Martin, J.M. and Nougaro, J., (Water level and distribution of discharge along a sideweir in a channel). Comptes Rendm Hebdomadaires des Seances de l' Acadenic des Sciences, Series A, Science Mathe matiague, 264, 14, 644-647 (Apr.-1967).
- 5. G. De Marchi: Saggio di teoria del funzionamento degli stramazzi laterali (Essay of the performance of lateral weirs), L'Energia elettrica, Milano, vol. 11, no. 11, pp. 849-860, November, 1934; reprinted as Istituto di Idraulica e Costruzioni Idrauliche, Milano, Memorie e studi No. 11, 1934.
- 6. G. De Marchi: Profili longitudinali della superficie libera delle correnti permanenti lineari con portata progressivamente crescente o progressivamente decrescente entro canali di sezione costante (Longitudinal flow profiles of linear steady flow with increasing discharges or decreasing discharges in prismatic channels), Ricerca scientifica e ricostruzione, Rome, nos. 2 and 3, pp.202-216, February-March, 1947. Also published as Des formes de la surface libre de courants permanents avec debit progressivement croissant ou progressivement decroissant dans un canal de section constante, Revue generale de l'hydraulique, Paris, vol. 13, no. 38, pp. 81-85, 1947.
- Hubert Engels: Mitteilungen aus dem Dresdener Flussbau-Laboratorium (Report of the Dresden Hydraulic Laboratory). Zeitschrift des Vereins deutscher Ingenieure, Berlin, vol. 62, no. 24, pp. 362-365, June 15; no. 25, pp. 387-390. June 22; no. 26, pp. 412-416, June 29, 1918; and vol. 64, no. 5, pp. 101-106, Jan. 31, 1920; also Forschungsarbeiter auf dem Gebiete des Ingenieurwesens, Berlin, nos. 200 and 201, 55 pp., 1917.

<sup>\*</sup> References in page 49 are to be read alongwith this list

- 8. Favre, H.' Contribution a' l' e' tude des contrants liquides,' Zurich 1923.
- 9. Frank's Jos, 'Sicherung der Werkkanale gegen eindringendes Hochwasser,' Wassercraft and Wasserwirtshaft, 1941, Vol. 1, p. 12
- B. Gentilini: Ricerche sperimentali sugli sfioratori longitudinali (Experimental researches on side weirs), L'Energia elettrica, Milano, vol. 15, no. 9, pp.583-595, September, 1938; reprinted as Istituto di Idraulica e Costruzioni Idrauliche, Milano, Memorie e studi No. 65, 1938.
- Mc Nown Johns and Hsu En-Yun, 'Application of Conformal Mapping to Divided Flow,' Proc. the Midwestern Conference on Fluid Dynamics, First Conference, 1950.
- 13. Musterle, T, 'The calculation of Water levels without Parameters for side-weirs' (in German) -Wasserwirtschaft, 585, 145-149- (May 1968).
- 14. Parmley, W.L., The Walworth Sewer, Cliveland, Ohio, Tran. Am. Soc. Civ. Engrs, Vol. 55, 1905, 2. 341.
- 15. Peter, Y., 'Problem of Side-spillways', Civil Engrs (London) V. 56 n 657 March 1961 p. 327, 329-30 Apr.490-2.
- Martin Schmidt: Zur Frage des Abflusses über Streichwehre (Discharge over side weirs), Technische Universität Berlin-Charlottenburg, Institut für Wasserbau, Eitteflung 41, 1954.
- Martin Schmidt: Die Berechnung von Streichwehren (Computation of side weirs), Die Wasserwirtschaft, Stuttgart, vol. 45, no. 4, pp. 96-100, January, 1955.
- 18. Martin Schmidt: 'Gerinnehydraulik' ('Open-channel Hydraulics' VEB Verlag Technik, Berlin, and Bauverlag GMBH, Wiesbaden, 1957, pp. 188-196.
- 19. Tults H., 'Flood Protection of Canals by Lateral spillways,' Am. Soc. Civ. Engrs. -Proc., V. 82, (J. Hyd. Division, n Hy 4 Oct. 1956 p. 1077, 17 p.
- 20. Tyler, R.G., Carolle, J.A. and Steskal N.A. 'Discharge over Side-Weirs with and without Baffles,' J.Boston Soc. Civ. Engrs. Vol. 16, 1929, p. 118.

APPENDIX A

EXPERIMENTAL DATA

#### APPENDIX A

## EXPERIMENTAL DATA

#### A-1 FLUME A

Sera-	Ex. No.	L (cms)	B (cms)	s (cms)	y <sub>1</sub> (ems)	y <sub>2</sub> (cms)	Q <sub>s</sub> (litres/ sec.)	Q1 (Litres/ sec.)
AA	<b>1</b> 2 3 4	10.180 10.180 10.180 10.180	61.277 61.277 61.277 61.277	50.902 50.902	65.623 58.552 53.188 62.514	58.308 53.188	3.771 0.654	33.913 34.836 34.264 19.253
<b>A</b> I	56789101 112314	10.180 10.180 20.330 20.330 20.330 20.330 20.330 20.330 20.330	61.277 61.277 61.277 61.277 61.277 61.277 61.277	50.902 50.902 50.902 50.902 50.902 50.902 50.902	57.729 54.376 58.979 53.889 58.979 53.919 53.950 53.950	54.285 58.918 53.736 58.918 58.979 53.858 53.889 53.980	1.196 8.267 1.954 8.235 8.235 8.283 1.948 1.961 1.995	18.935 18.901 18.707 18.218 28.554 16.423 42.105 28.542 57.928 70.007
	15 16 17 18 19 20 21 22 23 24	20.330 20.330 20.330 20.330 20.330 20.330 20.330 20.330 20.330	61.277 61.277 61.277 61.277 61.277 61.277	50.902 50.902 50.902 50.902 38.222 38.222 38.222	59.009 56.937 59.893 63.642 40.264 40.264 40.264 42.459	56.93° 56.93° 59.863 63.646 40.17° 40.17° 40.17° 42.39°	7 5.475 7 5.438 3 9.811 2 16.097 3 1.126 3 1.107 3 1.146 8 3.246	64.095 40.497 72.172 45.324 50.521 48.715 72.747 17.433 53.263 59.739
	25 26 27 28 29 30 31 32 334	20.330 20.330 20.330 20.330 20.330 20.330 20.544 20.544	61.277 61.277 61.277	38. 222 38. 222 38. 222 38. 222 38. 222 25. 48	2 50.993 2 50.993 2 54.590 2 58.826 1 26.853 1 26.73	42.42 47.82 50.99 50.99 54.62 58.82 26.85 26.57	8 3.218 3 10.587 3 15.861 3 16.026 0 23.089 6 32.448 3 0.613 0 522	24.660 72.916 64.991 72.342 34.751 38.600 44.079 46.726 69.205 68.375

wyerrestarophysical	Ex.	L						
erı-	No.	(cms)	B (cms)	(cms)	y <sub>1</sub> (cms)	y <sub>2</sub> (cms)	Q <sub>s</sub> (Litres/	Q <sub>1</sub> (litres/
≟B,	35	20.544	61.277	25.481	28.285	28.255	sec.)	sec.) 44.459
•	36 37 38	20.544 20.544 20.544	61.277 61.277	25.481 25.481 25.481	30.053 29.962	30.084 30.023	3.712 3.460	44.2 <b>7</b> 8 67.575
	39 40 41	20.544 20.544	61.277 61.277	25.481 25.481	31.791 31.852 33.924	31.852 31.882 33.985	5.987 9.137	68.290 43.544 44.009
	42 43	20.544 20.544 20.544	61.277	25.481 25.481 25.481	33.955 36.393 39,197	34.046 36.515 39.319	9.003 13.045 18.109	67.759 68.038 67.709
	44	20.544	61.277	25.481	42.459	42.611	24.645	69.746
	45 46 47.	20.452 20.452 20.452	61.277 61.277 61.277	10.119 10.119 10.119	10.942 11.918 12.649	10.942 11.918 12.649	0.886	34.425 34.130 49.263
	48 49 50	20.452 20.452 20.452	61.277 61.277 61.277	10.119	12.649 13.503 13.503	12.649 13.442	1.492 1.752	33.475 55.475 45.821
	<b>51</b> 52	20.452 20.452	61.277 61.277	10.119	14.508 14.417	13.503 14.508 14.417	2.595 3.057	60.486 46.90 <b>1</b>
	53 54	20.452 20.452	61.277 61.277	10.119	15.575 15.575	15.636 15.636	4.531 4.047	46.382 61.129
	55 56	20.452	61.277	10.119	16.886	17.069	5.728	70.109 69.359
	57 58 59	20.452 20.452 20,452	61.277 61,277 61.277	10.119 10.119 10.119	16.947 16.855 20.269	17.160 16.855 20.269	6.321	61.494 45.950 45.729
	60 61	20,452 20,452	61.277 61.277	10.119	20.269 25.298	20.269 25.298	11.437	61.315 61.311 60.809
	62 63 64	20.452 20.452 20.452	61.277 61.277 61.277	10.119	33.680 33.680 25.298	33.680	39.832 39.791 20.674	70.809 70.645
	65 66	20.452 20.452	61.277 61.277	10.119	20.269 10.241	20.269 10.942	11.016	70.595 44.492
	67 68	20.452 20.452	61.277 61.277 61.277	0.000	10.241 17.160	10.729 17.496	11.417 25.540 34.872	32.506 45.587 45.238
	69 70 7 <b>1</b>	20.452 20.452 20.452	61.277 61.277	0.000	8.230 16.551	8.992 <b>1</b> 6.703	7.706 3 24.859	29.724 29.291
	72 73 74	20.452 20.452 20.452	61.277 61.277 61.277	0.000	11.186 19.964 16.032	20.086	12.085 32.197 22.738	55.159 52.926 52.762

	Ex.	$\Gamma$	D					
Seri- es		(cms)	B (cms)	s (cms)	y <sub>1</sub> (cms)	y <sub>2</sub> (cms)	Q <sub>s</sub>	Q <sub>1</sub> (Litres/
***************************************	all the manufacture and a second			~~~	(05)	(Omb)	sec.)	sec.)
<b>Æ</b> .	75 76 77 78 79 80 <b>81</b> 82 83	20.452 20.452 20.452 20.452 20.452 20.452 20.452 20.452 20.452	61.277 61.277 61.277 61.277 61.277 61.277 61.277 61.277	0.000 0.000 0.000 0.000 0.000 0.000	24.079 12.283 10.058 10.485 4.298 5.639 10.455 20.361 20.361 16.581	11.034 20.330	2.668 9.393 33.135 33.135	51.821 58.974 46.840 50.275 46.728 48.032 48.900 48.508 48.508 48.622
	85 86 37 89 90 91 934	20.452 20.452 20.452 20.452 20.452 20.452 20.452 20.452 20.452	61.277 61.277 61.277 61.277 61.277 61.277 61.277 61.277	0.000 0.000 0.000 0.000 0.000 0.000	12.070 17.800 6.157 11.278 15.270 22.494 6.492 5.456 4.054 6.858	17.770 6.309 11.735 16.185 22.951 6.523 5.182 3.993	5.563 9.864 21.284 38.267 3.237 2.362 1.568	63.854 65.007 11.125 57.724 58.762 57.226 56.717 70.373 66.985 70.977
	95 96 97 98 99 101 102 103 104	20.452 20.452	61.277 61.277 61.277 61.277 61.277		7.529 7.315 6.340 13.045 14.691 13.553 11.552 10.668 11.674	6.858 5.974 12.984 15.118 14.173 11.704 11.605 12.253	3 4.141 2.454 11.092 3 18.008 5 16.192 4 9.723 7 8.852 5 12.920	71.185 62.847 61.724 72.231 72.755 56.841 56.682 47.677 47.754 53.429
	106	20.452 20.452 20.452	51.277	0.000 0.000 0.000	10.820 12.924 13.899	12.588	1 9.290 3 10.624 3 15.052	52.705 71.815 72.336
AC.	10 <b>9</b> 110 111 112 113 114 115	38.130 38.130 38.130 38.130	61.277 61.277 61.277 61.277 61.277 61.277	7 0.000 7 0.000 7 0.000 7 0.000 7 0.000 7 0.000 7 0.000 7 0.000	8.108 9.510 11.003 12.10 10.947 11.278 11.88' 13.228 15.977	0 10.33; 3 11.67; 1 12.71; 2 9.35; 3 12.55; 7 13.41; 8 14.35; 2 16.55	3 17.957 4 23.680 5 28.139 7 12.837 8 20.839 1 24.890 5 30.680 1 42.354	37.301 37.576 37.839 37.932 57.328 58.200 56.130 56.470 56.165 70.502

~-	Ex.	L	В					
Seri- es	No.	(cms)	(cms)	s (cms)	y <sub>1</sub> (cms)	y <sub>2</sub> (cms)	Qs (Litres sec.)	Q <mark>1</mark> / (Litres/ sec.)
AC	118 119 120 121 122 123 124 125 126 127	38.130 38.130 38.130 38.130 38.130 38.130 38.130 38.130 38.130	61.277 61.277 61.277 61.277 61.277 61.277 61.277 61.277	0.000 0.000 0.000 0.000 0.000 0.000 0.000	13.472 14.661 16.307 19.050 8.473 7.315 6.157 5.243 4.298 4.115	14.996 16.063 17.343 19.964 8.626 7.041 6.157 5.608 4.968 4.694	29.005 34.275 41.976 51.258 12.045 7.448 5.753 4.443 2.953 3.191	72.122 71.363 71.083 70.049 70.495 69.271 69.170 68.990 72.707 60.173
	128	38.130	61.277	0.000	5 <b>.3</b> 3 '	5 <b>.7</b> 30	4.432	61.414
<b>A</b> D	129 130 131 132 133 134 136 137 138	61.021 61.021 61.021 61.021 61.021 61.021 61.021 61.021 61.021	61.277 61.277 61.277 61.277 61.277 61.277 61.277 61.277	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	9.083 9.114 9.601 11.034 14.143 6.980 4.999 3.871 11.430 11.796	5.883 9.906 10.820 11.918 15.210 6.279 5.273 4.298 6.767 10.333	54.551 12.105 6.935 4.815 16.503	43.606 44.034 43.579 42.791 61.316 53.997 52.475 50.486 60.605 61.228
	139 140 141	61.021 61.021 61.021	61,277 61.277 61.277	0.000 0.000 0.000	13.746 13.929 7.529	9.449 15.728 7.163	43.202	77.401 78.186 75.909
Au	142 143 144 145 146 147 148 150 151	38.100 38.100 38.100 38.100 38.100 38.100 38.100 38.100 38.100	61.277 61.277	21.519 21.519 8.016 8.016	28.103 31.852 15.423 19.568 22.128	30.876 29.047 28.438 32.095 16.459 20.726 26.243	38.704	99.650 100.001 89.938 89.094 51.198 51.480 86.381 86,733 84.956 41.512
	152 153 154 155• 156	38.100 38.100 38.100 38.100 38.100	61.277 61.277 61.277 61.277 61.277	8.016 8.016 8.016 8.016 8.016	13.533 12.924 <b>15.</b> 8 <b>5</b> 0	13.716 13.442 16.764	29.648 8.219 7.300 13.531 23.030	41.298 40.847 50.715 86.444 85.647

~								
Seri es	L- Ex. No.	( <sup>T</sup> ms)	B (cms)	s (cms)	y <sub>1</sub> (cms)	y <sub>2</sub> (cms)	Qs (Litres sec.)	Q <sub>1</sub> s/ (Litre: sec.
AF	157 158 159 161 162 163 164 165	60.960 60.960 60.960 60.960 60.960 60.960 60.960	61.277 61.277 61.277 61.277 61.277 61.277 61.277 61.277	7.864 7.864 7.864 7.864 7.864 2.743 2.743 2.743	12.497 15.362 20.696 21.214 17.221 6.553 5.304 4.877 5.456	16.886 21.610 23.409 20.300 5.883 5.060	10.276 23.532 44.491 52.375 31.169 3.527 2.867 1.527 1.515	67.812 69.468 64.320 102.765 103.792 71.593 70.655 69.147 76.305
AG	DATA	OF THE H	YDRAULIC ;	UMP				
	166 167 168 169 170 171 172 173	84.000 84.000 84.000 84.000 84.000 84.000 84.000	61.227 61.277 61.277 61.277 61.277 61.277 61.277	0.000 0.000 0.000 0.000 0.000 0.000 0.000	0.155 0.115 0.099 0.135 0.133 0.142 0.192 0.190	0.342 0.403 0.475 0.608 0.507 0.710 0.461 0.700	1.35 1.267 1.120 2.065 2.27 2.27 2.27 0.147	1.728 1.645 1.565 2.417 2.662 2.605 2.567 2.82
A-2	FLUME	<u>B</u>						
BA	<b>1</b> 23456789 <b>1</b> 0	5.100 5.100 5.100 5.100 5.100 5.100 5.100 5.100 5.100	24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	3.700 3.660 3.660 3.650 3.640 3.640 3.630 4.140 3.660	3.550 3.470 3.300 3.400 3.400 3.280 3.270 3.760 3.000	0.578 0.466 0.528 0.621 0.633 0.618 0.597 0.555 0.466	2. 196 3. 049 2. 518 1. 393 0. 722 1. 052 1. 775 2. 206 3. 311 3. 056
	11 12 13 14 15 16 17 18 19 20	5.100 5.100 5.100 5.100 5.100 5.100 5.100 5.100 5.100	24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	3.660 3.650 3.700 8.280 6.810 3.020 2.730 6.890 4.530 12.400	3.000 3.100 7.600 6.000 2.900 2.600 6.000 4.190 11.500	0.528 0.621 0.578 2.213 1.656 0.452 0.360 1.647 0.732 4.051	2.518 1.393 2.196 2.391 1.801 1.321 1.333 4.057 4.057 4.906
							60.	ntd

Serı-	Ex.		В	S		TV	$\cap$	0
	110.	(cms)	(cms)	(cms)	(cms)	y <sub>2</sub> (cms)	Qs (Litres/ sec.)	Q1 (Litres, sec.)
BB	21 22 23 24 25 26 27 28 29	9.960 9.960 9.960 9.960 9.960 9.960 9.960	24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800 24.800	0.000 0.000 0.000 0.000 0.000 0.000 0.000	3.680 3.670 3.670 3.670 3.670 3.690 3.680 3.680	3.470 3.500 3.380 3.510 3.480 3.500 3.360 3.340 3.300	1.201 0.985 1.025 1.101 1.126 1.147 1.174 1.178 1.193 1.202	1.516 3.175 3.022 2.723 2.488 2.264 2.033 1.769 1.647 1.316
	31 32 33 34 35 36	9.960 9.960 9.960 9.960 9.960	24.800 24.800 24.800 24.800 24.800 24.800	0.000 0.000 0.000 0.000 0.000	5.040 6.150 6.890 4.800 2.060 2.670	4.710 5.930 6.680 4.470 1.800 2.260	1.921 2.655 3.169 1.349 0.434 0.716	2.574 3.606 4.317 5.156 0.793 0.786
BC	37 38 40 41 42 43 44 45 46	15.000 15.000 15.000 15.000 15.000 15.000 15.000 15.000 15.000	24.800 24.800 24.800 24.800 24.800 24.800 24.800 17.550	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	3.670 3.670 3.670 3.680 3.660 3.680 4.290 3.950 3.440	3.320 3.330 3.380 3.430 3.480 3.510 3.570 4.450 3.300	1.738 1.731 1.717 1.697 1.681 1.587 1.419 1.609 1.890 1.1516	1.850 2.101 2.322 2.553 2.851 3.041 3.574 5.004 2.730 2.138
	47 49 55 55 55 55 55 56	15.000 15.000 15.000 15.000 15.000 15.000 15.000 15.000	17.550 17.550 17.550 17.550 17.550 17.550 17.550 17.550 17.550	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	2.820 1.940 3.940 4.220 3.750 3.400 3.790 3.530 3.940 3.790	2.530 1.590 3.800 4.260 3.640 3.600 3.600 3.840 3.710	1.075 0.583 1.218 1.351 1.218 1.390 1.819 1.559 1.417	1.459 0.737 3.086 3.564 3.012 2.252 2.253 2.185 2.653 2.848
	57 58 59 61 62	15.000 15.000 15.000 15.000 15.000	17.550 17.550 17.550 17.550 17.550 17,550	0.000 0.000 0.000 0.000 0.000	3.850 3.860 4.050 4.120 4.230 4.640	3.820 3.820 4.060 4.050 4.040 4.770	1.674 1.473 1.580 1.384 1.390 1.533	2.777 2.954 3.238 3.398 3.569

# NON DIMENSIONAL PARAMETERS

A-3 FLUME A

	Tiberes				
Series	Exp.	h <sub>1</sub> /L	L/B	s/y <sub>1</sub>	F <sub>1</sub>
AA	1 2 3 4	1.4461 0.7515 0.2246 1.1407	0.1661 0.1661 0.1661 0.1661	0.7757 0.8693 0.9570 0.8142	0.0332 0.0405 0.0460 0.0203
AB	5 6 7 8 9 10 11 12 13 14	0.6707 0.3413 0.3973 0.1469 0.3943 0.3973 0.1484 0.1469 0.1499	0.1661 0.1661 0.3318 0.3318 0.3318 0.3318 0.3318 0.3318 0.3318	0.8817 0.9361 0.8630 0.9446 0.8639 0.8630 0.9440 0.9446	0.0225 0.0246 0.0215 0.0240 0.0329 0.0189 0.0554 0.0376 0.0762
	15 16 17 18 19 20 21 22 23 24	0.3988 0.2969 0.2969 0.4423 0.6267 0.1004 0.1004 0.1004 0.2084 0.3343	0.3318 0.3318 0.3318 0.3318 0.3318 0.3318 0.3318 0.3318 0.3318	0.8626 0.8940 0.8940 0.8499 0.7998 0.9493 0.9493 0.9002 0.8490	0.0737 0.0491 0.0875 0.0509 0.0518 0.0993 0.1484 0.0356 0.1003
	25 26 27 28 29 30 31 32 33	0.2084 0.2084 0.4723 0.6282 0.6282 0.8051 1.0135 0.0668 0.0608	0.3318 0.3318 0.3318 0.3318 0.3318 0.3318 0.3353 0.3353	0.9002 0.9002 0.7992 0.7496 0.7496 0.7002 0.6497 0.9489 0.9532 0.8989	0.0464 0.1373 0.1024 0.1035 0.0497 0.0499 0.0509 0.1750 0.2609 0.2361
	35 36 37 38 39 40	0.1365 0.2226 0.2181 0.3071 0.3101 0.4110	0.3353 0.3353 0.3353 0.3353 0.3353	0.9009 0.8479 0.8505 0.8015 0.8000 0.7511	0.1540 0.1'00 0.2147 0.1985 0.1262 0.1161 contd

A-3 FLUME A

Series	Exp.				
Dettes	No.	h <sub>1</sub> /L	L/B	s/y <sub>1</sub>	F <sub>1</sub>
AB	41 42 43 44	0.4125 0.5312 0.6677 0.8264	0.3353 0.3353 0.3353 0.3353	0.7504 0.7002 0.6501 0.6001	0.1784 0.1615 0.1438 0.1314
	45 46 47 48 49 50 51 52 54	0.0402 0.0879 0.1237 0.1654 0.1654 0.2146 0.2101 0.2668 0.2668	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	0.9248 0.8491 0.8000 0.8000 0.7494 0.7494 0.6975 0.7019 0.6497	0.4956 0.4322 0.5706 0.3877 0.5826 0.4812 0.5703 0.4464 0.3932 0.5182
	55678901234	0.2653 0.3308 0.3338 0.3294 0.4963 0.4963 0.7422 1.1520 1.1520 0.7422	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	0.6510 0.5993 0.5971 0.6004 0.4992 0.4992 0.4000 0.3005 0.3005	0.5960 0.5208 0.4593 0.3460 0.2611 0.3501 0.2511 0.1621 0.1881 0.2893
	65 667 69 71 72 74	0.4963 0.5007 0.5007 0.8390 1.0283 0.4024 0.8092 0.5469 0.9762 0.7839	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	0.4992 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.4031 0.7073 0.5168 0.3341 0.2444 0.6560 0.2267 0.7682 0.3091 0.4282
	75 76 77 78 <b>79</b> 80 81 82. 83	1.1773 0.6006 0.4918 0.5127 0.2101 0.2757 0.5112 0.9955 0.9955 0.8107	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.2285 0.7138 0.7651 0.7715 2.7327 1.8690 0.7537 0.2751 0.2751 0.3752 contd

Series	Exp. No.	h <sub>1</sub> /L	L/B	g/T	T7.
ÀВ	85 86 87 88 89 90 91 92 93	0.5902 0.8703 0.3010 0.5534 0.7466 1.0999 0.3174 0.2668 0.1982 0.3352	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	s/y <sub>1</sub> 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	F <sub>1</sub> 0.7934 0.4510 0.3794 0.7942 0.5131 0.2795 1.7865 2.8772 4.2761 0.0592
	95 96 97 98 99 100 101 102 103	0.3681 0.3577 0.3100 0.6379 0.7183 0.6617 0.5648 0.5216 0.5708 0.5931	0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338 0.3338	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	1.7955 1.6551 2.0147 0.7987 0.6732 0.5949 0.7522 0.7129 0.6238 0.6589
	105 106 107	0.5291 0.6 <b>31</b> 9 0.6 <b>79</b> 6	0.3338 0.3338 0.3338	0.0000 0.0000 0.0000	0.7715 0.805+ 0.7274
AC	108 109 110 111 112 113 114 115 116 117	0.2126 0.2494 0.2886 0.3173 0.2870 0.2958 0.3118 0.3469 0.4189 0.3333	0.6223 0.6223 0.6223 0.6223 0.6223 0.6223 0.6223 0.6223	0.0700 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.8419 0.6676 0.5402 0.4695 0.8252 0.8007 0.7136 0.6116 0.4585 0.8107
	118 119 120 121 12 <b>8</b> 123 124 125 126 127	0.3533 0.3845 0.4277 0.4996 0.2222 0.1918 0.1615 0.1375 0.1127 0.1079	0.6223 0.6223 0.6223 0.6223 0.6223 0.6223 0.6223 0.6223 0.6223	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.7599 0.6624 0.5624 0.4390 1.4892 1.8242 0.3591 0.9946 4.2520 3.7562

4-3 FLUNE 4

Series	Exp. Np.	h <sub>1</sub> /L	L/B	s/y <sub>1</sub>	F <sub>1</sub>
AC	128	0.1399	0.6223	0.0000	2.5975
ΑD	\$29 130 131 132 133 134 135 136 137	0.1489 0.1494 0.1573 0.1808 0.2318 0.1144 0.0819 0.0634 0.1873 0.1933	0.9958 0.9958 0.9958 0.9958 0.9958 0.9958 0.9958 0.9958	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.8300 0.8339 0.7632 0.6083 0.6007 1.5257 2.4465 3.4540 0.8172 0.7875
	139 140 141	0.2253 0.2283 0.1234	0.9958 0.9958 0.9958	0.0000 0.0000 0.0000	0.7913 0.7836 1.9147
AВ	142 143 144 145 146 147 148 150 151	0.3056 0.4128 0.2352 0.1896 0.1728 0.2712 0.1944 0.3032 0.3704 0.2576	0.6218 0.6218 0.6218 0.6218 0.6218 0.6218 0.6218 0.6218 0.6218	0.6489 0.5777 0.7060 0.7487 0.7657 0.6756 0.6198 0.4097 0.3623 0.4496	0.2719 0.2292 0.2785 0.3013 0.1791 0.1492 0.7431 0.5221 0.4252 0.2873
	152 153 154 155 156	0.3280 0.1448 0.1288 0.2056 0.2864	0.6218 0.6218 0.6218 0.6218 0.6218	0.3908 0.5923 0.6203 0.5058 0.4235	0.2316 0.4275 0.5688 0.7138 0.5419
AF	1578 1599 1661 1662 1665	0.0760 0.1230 0.2105 0.2190 0.1535 0.0625 0.0420 0.0350 0.0445	0.9948 0.9948 0.9948 0.9948 0.9948 0.9948 0.9948 0.9948	0.6293 0.5119 0.3800 0.3707 0.4566 0.4186 0.5172 0.5625 0.5028	0.7998 0.6012 0.3560 0.5480 0.7567 2.2236 3.0142 3.3454 3.1198

nethodoxyddianichaeth difeirigaying doxyd charachaegan	Dan					
Series	Exp. No.	h <sub>1</sub> /L	L/B	s/y <sub>1</sub>	F <sub>1</sub>	
ĐÃ.	DATA (	F THE HYD	RAULIC JUME			
	166 167 168 169 170 171 172	0.077 0.057 0.048 0.067 0.066 0.071 0.096 0.05	1.375 1.375 1.375 1.375 1.375 1.375 1.375	0.0 0.0 0.0 0.0 0.0 0.0 0.0	2.48 3.70 4.43 4.27 4.82 4.23 2.68 2.99	
A-4 FLUI	WE B					
BA	1 2 3 4 5 6 7 8 9 1	0.7255 0.7176 0.7176 0.7157 0.7137 0.7137 0.7118 0.8118 0.7176	0.2056 0.2056 0.2056 0.2056 0.2056 0.2056 0.2056 0.2056	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	0.3973 0.5606 0.4630 0.2573 0.1339 0.1949 0.3290 0.4106 0.5060 0.5620	
	11 12 13 14 15 16 17 18 19 20	0.7176 0.7157 0.7255 1.6235 1.3353 0.5922 0.5353 1.3510 0.8882 2.4314	0.2056 0.2056 0.2056 0.2056 0.2056 0.2056 0.2056 0.2056 0.2056	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.4630 0.2573 0.3973 0.1292 0.1305 0.3241 0.3806 0.2888 0.5436 0.1447	
BB	21 22 23 24 25 26 27 29 30	9.3695 0.3695 0.3685 0.3685 0.3685 0.3705 0.3695 0.3695	0.4016 0.4016 0.4016 0.4016 0.4016 0.4016 0.4016 0.4016 0.4016	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	0.2765 0.5790 0.5534 0.4967 0.4556 0.4145 0.3692 0.3239 0.3004 0.2400	
	31	0.5060	0.4016	0.0000	0.2929 cont	d.,

Series	Exp.	h <sub>1</sub> /L	L/B	s/y <sub>1</sub>	F	
ÎΒ	32 33 34 35 36	0.6175 0.6918 0.4819 0.2068 0.2681	0.4016 0.4016 0.4016 0.4016 0.4016	0.0000 0.0000 0.0000 0.0000 0.0000	0.3044 0.3073 0.6312 0.3453 0.2319	o <u>agra</u> nda dhu uthan et
RC	33344 444 4456	0.2417 0.2447 0.2447 0.2453 0.2467 0.2440 0.2453 0.2860 0.2633 0.2293	0.6048 0.6048 0.6048 0.6048 0.6048 0.6048 0.6048 0.8547	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.3387 0.3846 0.4251 0.4655 0.5157 0.5591 0.6518 0.7250 0.6326 0.6096	
	47890123456 555555	0.1880 0.1293 0.2627 0.2813 0.2500 0.2267 0.2527 0.2353 0.2627	0.8547 0.8547 0.8547 0.8547 0.8547 0.8547 0.8547 0.8547 0.8547	0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000	0.5607 0.4962 0.7179 0.7479 0.7547 0.6534 0.5556 0.5992 0.6172	
	57 58 59 60 61 62	0.2567 0.2573 0.2700 0.2747 0.2820 0.3093	0.8547 0.8547 0.8547 0.8547 0.8547 0.8547	0.0000 0.0000 0.0000 0.0000 0.0000	0.6688 0.7086 0.7228 0.7392 0.7462 0.7690	

APPENDIX B

A DESIGN PROBLEM

## APPENDIX B

In the field application of side-weir, two types of problems are met.

(a) Given upstream flow conditions  $(Q_1, y_1)$  the problem is to find length of the weir to spill over the required discharge  $Q_s$ . In this case the crest height may be decided upon a certain discharge (say  $Q_0$ ) in the main channel above which the weir can start functioning. The height of the weir crest will be given by the normal depth corresponding to  $Q_0$  which may be calculated by Mannings formula; viz.

$$Q_0 = \frac{1}{n} AR^{2/3} S_0^{1/2}$$
 in metric units (B-1)

(b) Given upstream flow conditions  $(Q_1, y_1)$ , length and height of the weir crest (L, s) the problem is to find the discharge  $Q_s$  passing over the weir. The solution involves a tedious trial and error procedure.

The following example illustrates the procedures of solving both the types of problems. The problem has also been solved on computer for efficient solution and the corresponding programmes are given.

Example: A long channel of rectangular section 2m wide is laid on a slope of 0.001 and is lined with concrete, n = 0.014. Two side-weirs are to be installed, of equal length and on opposite

flow reaches .6 m<sup>3</sup>/sec and are to discharge .15 m<sup>3</sup>/sec. when the upstream flow is .9 m<sup>3</sup>/sec. Determine the length of the weirs, and the height of their crests above the channel bed. If the length is now made equal to 2.0 m, the crest height remaining the same what will be the discharge over the weirs for the same upstream flow of .9 m<sup>3</sup>/sec.

Given 
$$B = 2.0 \text{ m; slope S}_0 = .001$$

n = .014,  $Q_b = the discharge in the channel when the weir starts operating = 0.6 m<sup>3</sup>/sec.$ 

 $Q_1$  = Final upstream discharge = 0.9 m<sup>3</sup>/sec.

# Solution (Part A)

Given  $Q_S = .15 \text{ m}^3/\text{sec.}$  To find L, the length of the weir Section factor  $Z = AR^{2/3} = \frac{nQ}{\sqrt{S_O}}$   $= \frac{0.014 \times .6}{\sqrt{0.01}} = .2655$ 

$$\sqrt{.001}$$
 $B^{8/3} = 2^{8/3} = 6.35$ 

$$AR^{2/3}/B^{8/3} = \frac{.2655}{6.35} = .0418$$

From the graph (ref. Chow V.T., 'Open channel Hydraulics' pp.130), the normal depth is given by  $y_n/B = .165$ ,  $y_n = .165x2 = .33$ So height of the weir crest, s = .33 m. The normal depth corresponding to upstream flow (.9m3/sec.),

$$AR^{2/3} = \frac{nQ}{\sqrt{S_0}} = .0418 \times \frac{.9}{.6} = .0628$$

From the graph

$$y_1/B = .22$$
  
 $y_1 = .44 \text{ m}$   
 $v_1 = \frac{Q_1}{Bxy_1} = \frac{.9}{2x.44} = 1.022 \text{ m/sec.}$ 

Specific energy  $E = y_1 + v_1^2/2g$ 

$$= .44 + \frac{(1.022)^2}{2x9.81} = .4962 m$$

Upstream Froude number

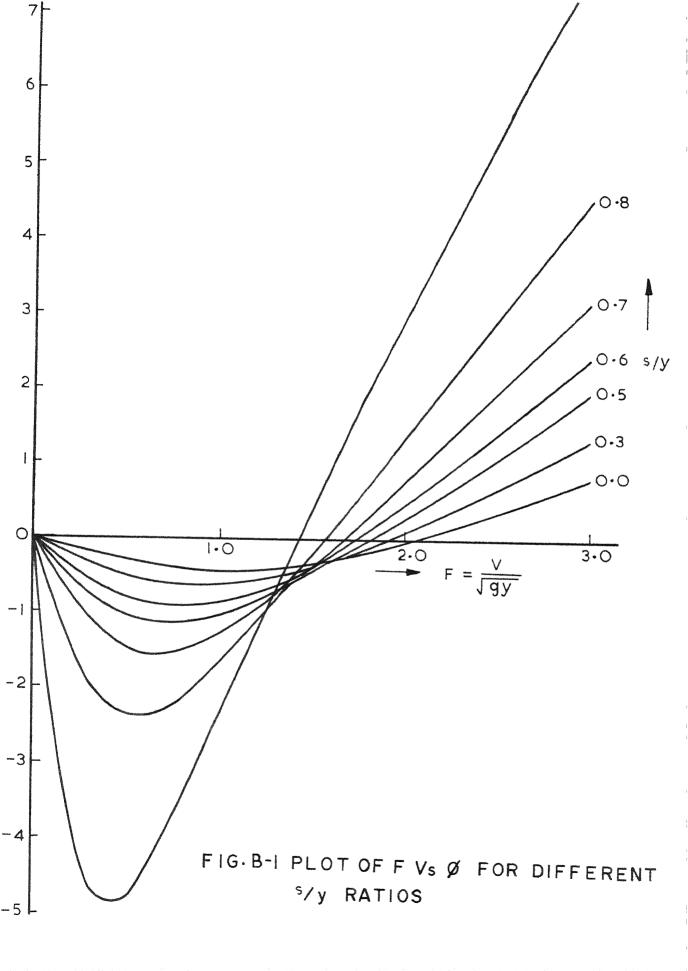
$$F_1 = \frac{V_1}{\sqrt{gy_1}} = \frac{1.022}{\sqrt{9.81 \times .44}} = .492$$

De Marchi equation for two weirs placed opposite to each other is

$$\frac{L}{B} = \frac{3}{4 \text{ C}_{M}} (\emptyset_{2} - \emptyset_{1})$$
 $s/y_{1} = .33/.44 = .75, F_{1} = .492$ 

From the Fig. B-1,

$$\emptyset_1 = -1.85$$
 $\emptyset_2 = Q_1 - Q_s = .9 - .15 = .75 \text{ m}^3/\text{sec.}$ 
 $E = y_2 + \frac{y_2^2}{2g} = y_2 + \frac{Q_2^2}{B^2 y_2^2 .2g}$ 



.4962 = 
$$y_2 + \frac{.75x.75}{y_2^2x 9x9.81}$$

or

$$.4962 = y_2 + \frac{.00717}{y_2^2}$$

Solving by trial and error method

$$y_2 = .4627 \text{ m}$$

$$s/y_2 = .33/.4627 = .713$$

$$F_2 = \sqrt{2(\frac{E}{y_2} - 1)} = \sqrt{2(\frac{.4962}{.4627} - 1)}$$

$$= .38$$
for  $F = .38$  and  $s/y = .713$ 

From Fig. B-1, for  $F_2 = .38$  and,  $s/y_2 = .713$ 

$$\phi_2 = -1.35$$

$$\emptyset_2 - \emptyset_1 = .50$$

$$C_{M} = .611 \sqrt{1 - \frac{3F_{1}^{2}}{F_{1}^{2} + 2}}$$
 (Ref. Eq. 4.11)

$$\frac{L}{B} = \frac{3}{4x \cdot 5} (.50) = .75$$

$$L = 1.5 m$$

Answer

## Solution Part II

Given 
$$L = 2.0 \text{ m i.e. } L/B = 1.0$$

To find Q,

Substituting in De Marchi equation

1.0 = 
$$\frac{3}{4x.5}$$
 ( $\emptyset_2$  - (-1.85))  
 $\emptyset_2$  = -1.85 + .667 = -1.183

A trial and error method has to be adopted to solve for  $\mathbf{y}_2$  and hence for  $\mathbf{Q}_{\mathbf{s}}.$ 

Step I assuming  $y_2 = .48$ 

$$s/y_2 = \frac{.33}{.48} = .687, \frac{E}{y_2} = \frac{.4962}{.48} = 1.033$$

$$E_2 = \sqrt{2(1.033-1)} = .257$$

From Fig. B-1

$$\phi_0 = -.90 > -1.183$$

Step II

$$y_2 = .468$$
  
 $s/y_2 = \frac{.33}{.468} = .705, E/y_2 = \frac{.4952}{.468} = 1.06$   
 $F_2 = \sqrt{2(1.06-1)} = .346$ 

From the Fig. B-1

$$\phi_2 = -1.25 < -1.183$$

Step III

$$y_2 = .472$$

$$s/y_2 = \frac{.33}{.472} = .70 \quad \frac{E}{y_2} = \frac{.4962}{.472} = 1.051$$

$$F_2 = \sqrt{2(1.051 - 1.0)} = .319$$

from Fig. B-1  $\phi_2 = -1.16 > -1.183$ 

Step IV

Assuming 
$$y_2 = .47$$
  
 $s/y_2 = \frac{.33}{.47} = .702$ ,  $E/y_2 = \frac{.4962}{.47} = 1.055$   
 $F_2 = \sqrt{2(E/y_2-1)} = \sqrt{2(1.055-1)} = .332$ 

from Fig. B-1

$$\emptyset_2 = -1.20 < -1.183$$

By interpolation  $y_2 = .4701$ 

$$Q_2 = B y_2 \sqrt{2g(E-y_2)}$$
  
= 2 x .4701  $\sqrt{2}$  x 9.81 (.4962 - .4701)  
= .635  $m^3/\text{sec}$   
 $Q_8 = Q_1 - Q_2 = .9 - .635 = .265$ 

$$Q_s = .265 \text{ m}^3/\text{sec.}$$
 Answer

## COMPUTER SOLUTION (PART A)

```
GIVEN Y1, Q1, S, QS, B, G TO FIND L, Y2
```

```
C
       N=NO. OF WEIRS
C
       Y1=UPSTREAM DEPTH, Q1=UPSTREAT FLOW, S=HEIGHT OF TEIR CREST
\mathbb{C}
     L=LENGTH OF WEIR. B=WIDTH OF CHANNEL G=ACCV DUE TO GRAVITY
       11=2
       AU=N
       REAL L
       PHI(F, ETA) = ((2.+F**2.-3.*ETA)/(1.+.5*F**2.-ETA))*SQRT(.5*F**2.-ETA)
      1(1.-ETA))-3.*ARSIN(SORT(.5*F**2./(1.+.5*F**2.-ETA)))
       READ 10, Y1, Q1, S, QS, B, G
       FORMAT (6F7.2)
  10
       F1=Q1/(Y1*B)/SQRT(G*Y1)
V1=Q1/(Y1*B)
       E=Y1+V1**2./(2.*G)
       IF(F1-1.)20,20,30
  20
       CM=.611*SORT(1.-3.*F1**2./(F1**2 +2))
       GO TO 40
       CM=.36-.08*F1
  30
       CONTINUE
  40
       ETA1=S/Y1
       Q2=Q1-QS
       PHI1=PHI(F1.ETA1)
       A=Q2**2./(2.*G*B*B)
        Y2=Y1
        DO 80 J=1,25
        F2=SQRT (2.*(E/Y2-1.))
        ET_2=S/Y2
        YLAST=Y2
        FX=Y2**3.-E*Y2**2.+A
        FDX=3.*Y2**2._2.*E*Y2
        Y2=Y2-FX/FDX
        IF(ABS(YL.ST-Y2).LE..OO01)GO TO 90
  30
        CONTINUE
  90
        CONTINUE
        PHI2=PHI(F2, ETA2)
        L=1.5+B*(PHI2-PHI1)/(CM*AU)
        PRINT 92, L, Y2
FORMAT (//20X, *LENGTH OF THE SIDE-WEIR=*, F7.4, /20X, *DOWN
  92
       1STREAM DEPTH=*, F7.4//////////
        STOP
        END
   SENTRY
                 .33 0.15 2.00 9.81
     . 44
            .90
```

#### EXECUTION

LENGTH OF THE SIDE-WEIR = 1.50 m DOWNSTREAM DEPTH = 0.4627

```
GIVEN V1. 01. S. L.B.G TO FIND QS. Y2
C
       N=NO. OF WEIRS
O
       Y1=UPSTREAM DEPTH.Q1=UPSTREAM FLOW. S=HEIGHT OF WEIR CREST
\alpha
     L=LENGTH OF WEIR.B=WIDTH OF CHANNEL, G=ACCN DUE TO GRAVITY
       AN=N
       REAL L
       PHI(F, ETA) = ((2. +F**2.-3.*ETA)/(1.+.5*F**2.-ETA))*SQRT(.5*F**2
      1(1.-ETA))-3.*ARSIN(SQRT(.5*F**2./(1.+.5*F**2.-ETA)))
       READ 10, Y1, Q1, S, L, B, G
       FORMAT(6F7.2)
F1=01/(Y1*B)/SQRT(G*Y1)
       V1=Q1/(Y1*B)
E=Y1+V1**2./(2.*G)
       IF(F1-1.)20,20,30
       CM=.611*SQRT(1.-3.+F1**2./(F1**2.+2.))
   20
        GO TO 40
        CM = .36 - .08 * F1
   30
        CONTINUE
   40
        ETA1=S/Y1
        R1=L/B
        PHI1=PHI(F1.ETA1)
        PHI2=AN*R1*CM/1.5+PHI1
        Y2=Y1
        DO 80 J=1,25
        F2=SQRT(2.*(E/Y2-1.))
        ETA2=S/Y2
        YLAST=Y2
        FX=PHI(F2,FTA2)-PHI2
        FDX=(3.*Y2-2.*E)/(2.*SQRT((E-Y2)*(Y2-S)**3.))
        Y2=Y2-FX/FDX
        IF(ABS(YLAST-Y2).LE..0001)GO TO 90
        CONTINUE
    80
        CONT INUE
    90
        02=F2*B*SQRT(G)*Y2**1.5
        OS=01-02
        PRINT 92,QS,Y2
       FORMAT (//20X, *TOTAL FLOW OVER THE WEIR=*, F7.4, /20X, *DOWNSTREAL
       1 DEPTH=*, F7.4///////////
        STOP
        END
 SENTRY
         .44 .90 .33 2.00 2.00 9.81
```

COMPUTER SOLUTION (PART B)

#### EXECUTION

TOTAL FLOW OVER THE WRIR = 0.2650 DOWNSTREAM DEPTH = 0.4701

# APPENDIX C

HYDRAULIC JUMP ALONG THE SIDE-WEIR

### APPENDIX C

# HYDRAULIC JUMP ALONG THE SIDE-WEIR

# C-1 Introduction:

In supercritical flow regime a hydraulic jump may for if the high velocity stream meets a subcritical stream of appropriate depth. It is possible for a hydraulic jump to to place in the zone of a side-weir also.

Under such circumstances some length of the weir spills
the flow which is supercritical in the channel and rest of the
length passes out the subcritical flow after the jump. The
discharge over the side-weir along its length is of highly
varied nature, and does not render for easy solution.

An exploratory study of the hydraulic jump was carried out mainly on the weir of zero height and with only one experiment on the weir of finite height. In all these experiments, it was not possible to obtain hydraulic jumps with normal front. It was observed that the front of the jump was inclined at an angle  $\theta'$  with the normal to the centre line of the channel. The value of  $\theta'$  was observed to be approximately  $45^{\circ}$  for weirs of zero height and small Froude numbers. The value of  $\theta'$  tended to decrease for high Froude numbers and finite height of weirs. No detailed study was done on the variation of  $\theta'$ .

## C-2 Analysis:

It was attempted to analyse the hydraulic jump occurring along the side-weir as an oblique jump. The value of  $\theta'$  was assumed as  $45^{\circ}$ . The classical oblique jump equation (3) is;

$$\frac{y_2}{y_1} = \frac{1}{2} \left( \sqrt{1 + 8F_1^{*2} - 1} \right) \tag{C-1}$$

where

$$F_1^* = F_1 \cos \theta$$
.

For the experimental data  $y_2/y_1$  has been plotted against  $F_1^*$  in fig. C-1. Also plotted is equation (C-1). It is seen that for low Froude numbers the experimental data follow closely the plot of equation (C-1). However, for high Froude numbers the points diverge up, leading to the conclusion that  $\theta$  decreases with increase in Froude number. The value of  $\theta$  is also decrease for finite height of weirs. It is felt that the variation of  $\theta$  should be expressible as

$$\theta' = \mathbf{fn}'(\mathbf{F}_1, \mathbf{s}/\mathbf{y}_2) \tag{C-2}$$

To find the exact form of equation (C-2) a detailed study is needed.

It was concluded that the hydraulic jump occurring along the side-weir cannot have a normal front. It could be analysed as an oblique jump (Eq. C-1). However, a detailed study is needed to express inclination  $\theta$  of the front in terms of the flow parameters, i.e.  $F_1$  and  $s/y_2$ .

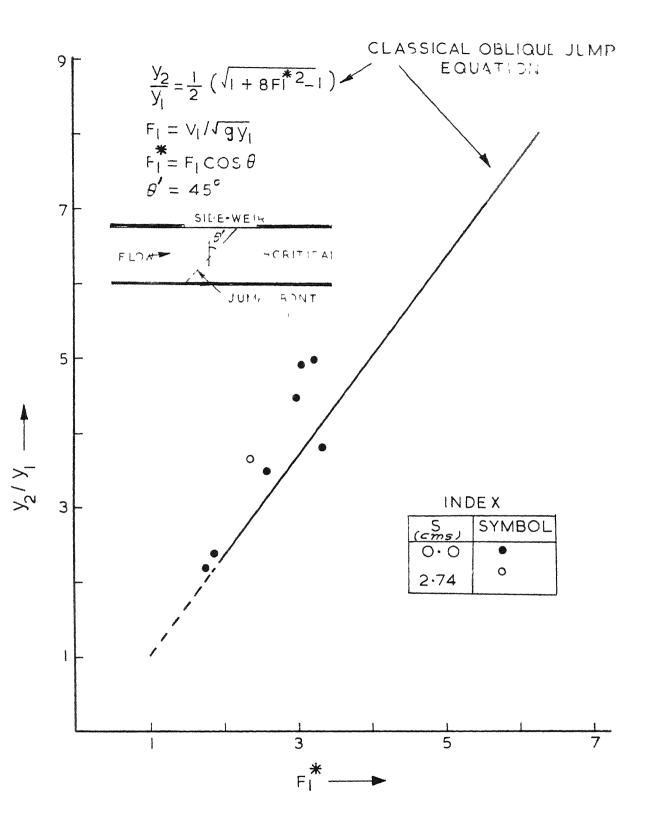


FIG. C-I HYDRAULIC JUMP ALONG A SIDE-WEIR

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Awasthy,
Hydraulic behavior
of side-weirs.